

Performance of the Barter, the Differential Evolution and the Simulated Annealing Methods of Global Optimization on Some New and Some Old Test Functions

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Introduction: The objective of this paper is to assess the performance of the Barter method, a newly introduced population-based (stochastic) heuristic to search the global optimum of a (continuous) multi-modal function, vis-à-vis that of two other well-established and very powerful methods, namely, the Simulated Annealing (SA) and the Differential Evolution (DE) methods of global optimization.

First we will describe the three methods briefly and then present the findings. The computer programs for DE and Barter methods are appended. The SA program (SIMANN) developed by William Goffe has been used to optimize the functions by the Simulated Annealing method.

The Simulated Annealing Method: The simulated annealing method (Kirkpatrick et al., 1983; Cerny, 1985) mimics the annealing process in metallurgy. In an annealing process a metal in the molten state (at a very high temperature) is slowly cooled so that the system at any time is approximately in thermodynamic equilibrium. As cooling proceeds, the system becomes more ordered – the liquid freezes or the metal re-crystallizes – attaining the ground state at $T=0$. This process is simulated through the Monte Carlo experiment (Metropolis et al. 1953). If the initial temperature of the melt is too low or cooling is done unduly fast the metal may become ‘quenched’ due to being trapped in a local minimum energy state (meta-stable state) forming defects or freezing out. The simulated annealing method of optimization makes very few assumptions regarding the function to be optimized, and therefore, it is quite robust with respect to irregular surfaces. In this method, the mathematical system describing the problem mimics the thermodynamic system. The current solution to the problem mimics the current state of the thermodynamic system, the objective function mimics the energy equation for the thermodynamic system, and the global minimum mimics the ground state. However, nothing in the numerical optimization problem directly mimics the temperature, T , in the thermodynamic system underlying the metallurgical process of annealing. Therefore, a complex abstraction mimics it. An arbitrary choice of initial value of a variable called ‘temperature’, how many iterations are performed at each ‘temperature’, the step length at which the decision variables are adjusted, and the rate of fall of ‘temperature’ at each step as ‘cooling’ proceeds, together make an ‘annealing schedule’. This schedule mimics the cooling process. At a high ‘temperature’ the step lengths at which the decision variables are adjusted are larger than those at a lower ‘temperature’. Whether the system is trapped into local minima (quenching takes place) or it attains the global minimum (faultless crystallization) is dependent on the said annealing schedule. A wrong choice of the initial ‘temperature’, or the rate of fall in the ‘temperature’ leads to quenching or entrapment of the solution in the local minima. The method does not provide any clear

guideline as to the choice of the ‘annealing schedule’ and often requires judgment or trial and error. If the schedule is properly chosen, the process attains the global minimum. It is said that using this method is an art and requires a lot of experience and judgment.

The Differential Evolution Method: The method of Differential Evolution (DE) grew out of Kenneth Price's attempts to solve the Chebychev Polynomial fitting Problem that had been posed to him by Rainer Storn. A breakthrough happened (1996), when Price came up with the idea of using vector differences for perturbing the vector population. The crucial idea behind DE is a scheme for generating trial parameter vectors. A population of points (p in d -dimensional space) is generated and evaluated (i.e. $f(p)$ is obtained) for their fitness. Then, in one of the schemes, for each point (p_i) three different points (p_a , p_b and p_c) are randomly chosen from the population. A new point (p_z) is constructed from those three points by adding the weighted difference between two points ($w(p_b - p_c)$) to the third point (p_a). Then this new point (p_z) is subjected to a crossover with the current point (p_i) with a probability of crossover (c_r), yielding a candidate point, say p_u . This point, p_u , is evaluated and if found better than p_i then it replaces p_i else p_i remains. Thus we obtain a new vector in which all points are either better than or as good as the current points. This new vector is used for the next iteration. In another (newly recommended) scheme, only two points are randomly chosen from the population and the third point is the p_i itself. Details set apart, this process makes the differential evaluation scheme completely self-organizing and effective in locating the global optimum.

The Barter Method: This method is based on the well-known proposition in welfare economics that competitive equilibria, under fairly general conditions, tend to be Pareto optimal [Takayama, 1974, pp. 185-201]. In its simplest version, implementation of this proposition may be outlined as follows [Mishra, 2006 (g)]:

Let there be n (fairly large number of) individuals in a population and let each individual, i , own (or draw from the environment) an m -element real vector of resources, $x_i = (x_{i1}, x_{i2}, \dots, x_{im})$. For every x_i there is a (single-valued) function $f(x_i)$ that may be used as a measure of the worth of x_i that the individual would like to optimize. The optimand function $f(\cdot)$ is unique and common to all the individuals. Now, let the individuals in the (given) population enter into a barter of their resources with the condition that (i) $\beta(x_{ij}, x_{k\ell} : i \neq k; j \neq \ell)$ or a transaction is feasible across different persons and different resources only, and (ii) the resources will change hands (materialize) only if such a transaction is beneficial to (more desired by) both the parties (in the barter). The choice of the individuals, (i, k) and the resources, (j, ℓ) in every transaction and the quantum of transaction would be stochastic in nature. If such transactions are allowed for a large number of times, then at the end of the session: (a) every individual would be better off than what he was at the initial position, and (b) at least one individual would reach the global optimum.

Computer Programs: A computer program (FORTRAN) that works out the global optimum of the test functions by the two methods (DE and Barter) is appended. It incorporated 87 benchmark functions of varied types, some well-known and others new (proposed by the present author). SIMANN, a global optimization algorithm using simulated annealing by William Goffe and others, is a very effective program written in FORTRAN-77. It may be downloaded from <http://www.netlib.no/netlib/opt/simann.f> absolutely free of cost.

The Findings: In all, benchmark functions have been optimized 89 times. As presented in table-1, the DE succeeds in 82 cases, the Barter succeeds in 63 cases, while the Simulated Annealing method succeeds for a modest number of 51 cases. The DE as well as Barter methods are unstable for stochastic functions (Yao-Liu#7 and Fletcher-Powell functions). In particular, Bukin-6, Perm-2 and Mishra-2 functions have been hard for all the three methods.

Seen as such, the barter method is much inferior to the DE, but it performs better than SA. A comparison of the Barter method with the Repulsive Particle Swarm method has indicated that they are more or less comparable [Mishra, 2006 (g)].

The convergence rate of the Barter method is slower than the DE as well as the SA. This is because of the difficulty of ‘double coincidence’ in bartering. Barter activity takes place successfully in less than one percent trials.

It may be noted that the DE and the SA have a longer history behind them and they have been improved many times. In the present exercise, the DE version used here employs the latest (available) schemes of crossover, mutation and recombination. In comparison to this, the Barter method is a nascent one. We need a thorough investigation into the nature and performance of the Barter method. We have found that when the DE optimizes, the terminal population is homogenous while in case of the Barter method it is not so. This property of the Barter method has several implications with respect to the Agent-Based Computational Economics [Tsfatsion, 2002].

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1: C      MAIN PROGRAM : PROVIDES TO USE BARTER METHOD, REPULSIVE PARTICLE
2: C      SWARM METHOD AND DIFFERENTIAL EVOLUTION METHOD.
3: C
4: C      ADJUST THE PARAMETERS SUITABLY IN SUBROUTINES DE, RPS AND BARTER
5: C      WHEN THE PROGRAM ASKS FOR PARAMETERS, FEED THEM SUITABLY
6: C
7: PROGRAM DERPSBART
8: IMPLICIT DOUBLE PRECISION (A-H, O-Z)
9: COMMON /KFF/KF,NFCALL,FTIT ! FUNCTION CODE, NO. OF CALLS & TITLE
10: CHARACTER *30 METHOD(3)
11: CHARACTER *1 PROCEED
12: CHARACTER *70 FTIT
13: COMMON /XBASE/XBAS
14: COMMON /RNDM/IU,IV ! RANDOM NUMBER GENERATION (IU = 4-DIGIT SEED)
15: INTEGER IU,IV
16: DIMENSION XX(3,50),KKF(3),MM(3),FMINN(3),XBAS(500,50)
17: DIMENSION X(50)! X IS THE DECISION VARIABLE X IN F(X) TO MINIMIZE
18: C      M IS THE DIMENSION OF THE PROBLEM, KF IS TEST FUNCTION CODE AND
19: C      FMIN IS THE MIN VALUE OF F(X) OBTAINED FROM DE OR RPS
20: WRITE(*,*) '----- WARNING ----- '
21: WRITE(*,*) 'ADJUST PARAMETERS IN SUBROUTINES DE, RPS & BARTER'
22: WRITE(*,*) 'FOR BARTER METHOD, DIMENSION MUST BE GREATER THAN ONE'
23: WRITE(*,*) '----- WARNING ----- '
24: METHOD(1)=' : DIFFERENTIAL EVOLUTION'
25: METHOD(2)=' : REPULSIVE PARTICLE SWARM'
26: METHOD(3)=' : BARTER ALGORITHM'
27: C      INITIALIZATION. THIS XBAS WILL BE USED IN ALL THREE PROGRAMS TO
28: C      INITIALIZE THE POPULATION.
29: WRITE(*,*) ' '
30: WRITE(*,*) 'FEED RANDOM NUMBER SEED [4-DIGIT ODD INTEGER] TO BEGIN'
31: READ(*,*) IU
32: C      THIS XBAS WILL BE USED IN ALL THE THREE METHODS AS INITIAL X
33: DO I=1,500
34: DO J=1,50
35: CALL RANDOM(RAND)
36: XBAS(I,J)=(RAND-0.5D00)*2000 ! RANDOM NUMBER BETWEEN (-1000, 1000)
37: ENDDO
38: ENDDO
39: WRITE(*,*) ' ***** '
40: C
41: DO I=1,3
42:
43: IF(I.EQ.1) THEN
44: WRITE(*,*) '===== WELCOME TO DE, RPS, BARTER GO PROGRAM ====='
45: WRITE(*,*) 'TO PROCEED TYPE ANY CHARACTER AND STRIKE ENTER'
46: READ(*,*) PROCEED
47: CALL DE(M,X,FMINDE,Q0,Q1) ! CALLS DE AND RETURNS OPTIMAL X AND FMIN
48: FMIN=FMINDE
49: ENDIF
50: C
51: IF(I.EQ.2) THEN
52: WRITE(*,*) ' '
53: WRITE(*,*) ' '
54: WRITE(*,*) '=====REPULSIVE PARTICLE SWARM PROGRAM ====='
55: WRITE(*,*) 'TO PROCEED TYPE ANY CHARACTER AND STRIKE ENTER'
56: C      READ(*,*) PROCEED
57: CALL RPS(M,X,FMINRPS,H0,H1) ! CALLS RPS AND RETURNS OPTIMAL X AND FMIN
58: FMIN=FMINRPS
59: ENDIF
60: C
61: IF(I.EQ.3) THEN
62: WRITE(*,*) ' '
63: WRITE(*,*) ' '
64: WRITE(*,*) '=====BARTER ALGORITHM PROGRAM ====='
65: WRITE(*,*) 'TO PROCEED TYPE ANY CHARACTER AND STRIKE ENTER'
66: C      READ(*,*) PROCEED
67: CALL BARTER(M,X,FMINEXC,G0,G1) ! CALLS RPS;RETURNS OPTIMAL X & FMIN

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68:      FMIN=FMINEXC
69:      ENDIF
70:
71: C -----
72:      DO J=1,M
73:      XX(I,J)=X(J)
74:      ENDDO
75:      KKF(I)=KF
76:      MM(I)=M
77:      FMINN(I)=FMIN
78:      ENDDO
79:      WRITE(*,' ')
80:      WRITE(*,' ')
81:      WRITE(*,'----- FINAL RESULTS=====')
82:      DO I=1,3
83:      WRITE(*,'FUNCT CODE=',KKF(I),' FMIN=',FMINN(I),' : DIM=',MM(I)
84:      WRITE(*,'OPTIMAL DECISION VARIABLES : ',METHOD(I)
85:      WRITE(*,'(XX(I,J),J=1,M)
86:      WRITE(*,'////////////////////////////////////')
87:      ENDDO
88:      WRITE(*,'OPTIMIZATION PROGRAM ENDED'
89:      WRITE(*,'*****')
90:      WRITE(*,'MEASURE OF EQUALITY/INEQUALITY'
91:      WRITE(*,'DE: BEFORE AND AFTER OPTIMIZATION = ',Q0,Q1
92:      WRITE(*,'RPS: BEFORE AND AFTER OPTIMIZATION = ',H0,H1
93:      WRITE(*,'BARTER: BEFORE AND AFTER OPTIMIZATION = ',G0,G1
94:      END
95: C -----
96:      SUBROUTINE DE(M,A,FBEST,G0,G1)
97: C PROGRAM: "DIFFERENTIAL EVOLUTION ALGORITHM" OF GLOBAL OPTIMIZATION
98: C THIS METHOD WAS PROPOSED BY R. STORN AND K. PRICE IN 1995. REF --
99: C "DIFFERENTIAL EVOLUTION - A SIMPLE AND EFFICIENT ADAPTIVE SCHEME
100: C FOR GLOBAL OPTIMIZATION OVER CONTINUOUS SPACES" : TECHNICAL REPORT
101: C INTERNATIONAL COMPUTER SCIENCE INSTITUTE, BERKLEY, 1995.
102: C PROGRAM BY SK MISHRA, DEPT. OF ECONOMICS, NEHU, SHILLONG (INDIA)
103: C -----
104: C PROGRAM DE
105:      IMPLICIT DOUBLE PRECISION (A-H, O-Z) ! TYPE DECLARATION
106:      PARAMETER (NMAX=500,MMAX=50) ! MAXIMUM DIMENSION PARAMETERS
107:      PARAMETER (RX1=0.0, RX2=0.5) ! TO BE ADJUSTED SUITABLY, IF NEEDED
108: C RX1 AND RX2 CONTROL THE SCHEME OF CROSSOVER. (0 <= RX1 <= RX2) <=1
109: C RX1 DETERMINES THE UPPER LIMIT OF SCHEME 1 (AND LOWER LIMIT OF
110: C SCHEME 2; RX2 IS THE UPPER LIMIT OF SCHEME 2 AND LOWER LIMIT OF
111: C SCHEME 3. THUS RX1 = .2 AND RX2 = .8 MEANS 0-20% SCHEME1, 20 TO 80
112: C PERCENT SCHEME 2 AND THE REST (80 TO 100 %) SCHEME 3.
113: C PARAMETER(NCROSS=2) ! CROSS-OVER SCHEME (NCROSS <=0 OR =1 OR =>2)
114:      PARAMETER(IPRINT=500, EPS=1.D-08) !FOR WATCHING INTERMEDIATE RESULTS
115: C IT PRINTS THE INTERMEDIATE RESULTS AFTER EACH IPRINT ITERATION AND
116: C EPS DETERMINES ACCURACY FOR TERMINATION. IF EPS= 0, ALL ITERATIONS
117: C WOULD BE UNDERGONE EVEN IF NO IMPROVEMENT IN RESULTS IS THERE.
118: C ULTIMATELY "DID NOT CONVERGE" IS REOPORTED.
119:      COMMON /RNDM/IU,IV ! RANDOM NUMBER GENERATION (IU = 4-DIGIT SEED)
120:      INTEGER IU,IV ! FOR RANDOM NUMBER GENERATION
121:      COMMON /KFF/KF,NFCALL,FTIT ! FUNCTION CODE, NO. OF CALLS * TITLE
122:      COMMON /XBASE/XBAS
123:      CHARACTER *70 FTIT ! TITLE OF THE FUNCTION
124: C -----
125: C THE PROGRAM REQUIRES INPUTS FROM THE USER ON THE FOLLOWING -----
126: C (1) FUNCTION CODE (KF), (2) NO. OF VARIABLES IN THE FUNCTION (M);
127: C (3) N=POPULATION SIZE (SUGGESTED 10 TIMES OF NO. OF VARIABLES, M,
128: C FOR SMALLER PROBLEMS N=100 WORKS VERY WELL);
129: C (4) PCROS = PROB. OF CROSS-OVER (SUGGESTED : ABOUT 0.85 TO .99);
130: C (5) FACT = SCALE (SUGGESTED 0.5 TO .95 OR 1, ETC);
131: C (6) ITER = MAXIMUM NUMBER OF ITERATIONS PERMITTED (5000 OR MORE)
132: C (7) RANDOM NUMBER SEED (4 DIGITS INTEGER)
133: C -----
134:      DIMENSION X(NMAX,MMAX), Y(NMAX,MMAX), A(MMAX), FV(NMAX)

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135:     DIMENSION IR(3),XBAS(500,50)
136: C
137: C ----- SELECT THE FUNCTION TO MINIMIZE AND ITS DIMENSION -----
138: CALL FSELECT(KF,M,FTIT)
139: C SPECIFY OTHER PARAMETERS -----
140: WRITE(*,*)'POPULATION SIZE [N] AND NO. OF ITERATIONS [ITER] ?'
141: WRITE(*,*)'SUGGESTED : N => 100 OR =>10.M; ITER 10000 OR SO'
142: READ(*,*) N,ITER
143: WRITE(*,*)'CROSSOVER PROBABILITY [PCROS] AND SCALE [FACT] ?'
144: WRITE(*,*)'SUGGESTED : PCROS ABOUT 0.9; FACT=.5 OR LARGER BUT <=1'
145: READ(*,*) PCROS,FACT
146: WRITE(*,*)'RANDOM NUMBER SEED ?'
147: WRITE(*,*)'A FOUR-DIGIT POSITIVE ODD INTEGER, SAY, 1171'
148: READ(*,*) IU
149:
150: NFCALL=0 ! INITIALIZE COUNTER FOR FUNCTION CALLS
151: GBEST=1.D30 ! TO BE USED FOR TERMINATION CRITERION
152: C INITIALIZATION : GENERATE X(N,M) RANDOMLY
153: DO I=1,N
154: DO J=1,M
155: C CALL RANDOM(RAND) ! GENERATES INITIATION X WITHIN
156: C X(I,J)=(RAND-.5D00)*2000 ! GENERATES INITIATION X WITHIN
157: C RANDOM NUMBERS BETWEEN -RRANGE AND +RRANGE (BOTH EXCLUSIVE)
158: X(I,J)=XBAS(I,J) ! TAKES THESE NUMBERS FROM THE MAIN PROGRAM
159: ENDDO
160: ENDDO
161: WRITE(*,*)'COMPUTING --- PLEASE WAIT '
162: IPCOUNT=0
163: DO 100 ITR=1,ITER ! ITERATION BEGINS
164: C -----
165: C EVALUATE ALL X FOR THE GIVEN FUNCTION
166: DO I=1,N
167: DO J=1,M
168: A(J)=X(I,J)
169: ENDDO
170: CALL FUNC(A,M,F)
171: C STORE FUNCTION VALUES IN FV VECTOR
172: FV(I)=F
173: ENDDO
174: IF(ITR.EQ.1) CALL GINI(FV,N,G0)
175: C -----
176: C FIND THE FITTEST (BEST) INDIVIDUAL AT THIS ITERATION
177: FBEST=FV(1)
178: KB=1
179: DO IB=2,N
180: IF(FV(IB).LT.FBEST) THEN
181: FBEST=FV(IB)
182: KB=IB
183: ENDDO
184: ENDDO
185: C BEST FITNESS VALUE = FBEST : INDIVIDUAL X(KB)
186: C -----
187: C GENERATE OFFSPRINGS
188: DO I=1,N ! I LOOP BEGINS
189: C INITIALIZE CHILDREN IDENTICAL TO PARENTS; THEY WILL CHANGE LATER
190: DO J=1,M
191: Y(I,J)=X(I,J)
192: ENDDO
193: C SELECT RANDOMLY THREE OTHER INDIVIDUALS
194: 20 DO IRI=1,3 ! IRI LOOP BEGINS
195: IR(IRI)=0
196:
197: CALL RANDOM(RAND)
198: IRJ=INT(RAND*N)+1
199: C CHECK THAT THESE THREE INDIVIDUALS ARE DISTICT AND OTHER THAN I
200: IF(IRI.EQ.1.AND.IRJ.NE.I) THEN
201: IR(IRI)=IRJ

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202:         ENDIF
203:         IF (IRI.EQ.2.AND.IRJ.NE.I.AND.IRJ.NE.IR(1)) THEN
204:             IR(IRI)=IRJ
205:         ENDIF
206:         IF (IRI.EQ.3.AND.IRJ.NE.I.AND.IRJ.NE.IR(1).AND.IRJ.NE.IR(2)) THEN
207:             IR(IRI)=IRJ
208:         ENDIF
209:         ENDDO ! IRI LOOP ENDS
210: C CHECK IF ALL THE THREE IR ARE POSITIVE (INTEGERS)
211:         DO IX=1,3
212:             IF (IR(IX).LE.0) THEN
213:                 GOTO 20 ! IF NOT THEN REGENERATE
214:             ENDIF
215:         ENDDO
216: C THREE RANDOMLY CHOSEN INDIVIDUALS DIFFERENT FROM I AND DIFFERENT
217: C FROM EACH OTHER ARE IR(1),IR(2) AND IR(3)
218: C ===== RANDOMIZATION OF NCROSS =====
219: C RANDOMIZES NCROSS
220: NCROSS=0
221: CALL RANDOM(RAND)
222: IF (RAND.GT.RX1) NCROSS=1 ! IF RX1=>1, SCHEME 2 NEVER IMPLEMENTED
223: IF (RAND.GT.RX2) NCROSS=2 ! IF RX2=>1, SCHEME 3 NEVER IMPLEMENTED
224:
225: C ----- SCHEME 1 -----
226: C NO CROSS OVER, ONLY REPLACEMENT THAT IS PROBABILISTIC
227:         IF (NCROSS.LE.0) THEN
228:             DO J=1,M ! J LOOP BEGINS
229:                 CALL RANDOM(RAND)
230:                 IF (RAND.LE.PCROS) THEN ! REPLACE IF RAND < PCROS
231:                     A(J)=X(IR(1),J)+(X(IR(2),J)-X(IR(3),J))*FACT ! CANDIDATE CHILD
232:                 ENDIF
233:             ENDDO ! J LOOP ENDS
234:         ENDIF
235:
236: C ----- SCHEME 2 -----
237: C THE STANDARD CROSSOVER SCHEME
238: C CROSSOVER SCHEME (EXPONENTIAL) SUGGESTED BY KENNETH PRICE IN HIS
239: C PERSONAL LETTER TO THE AUTHOR (DATED SEPTEMBER 29, 2006)
240:         IF (NCROSS.EQ.1) THEN
241:             CALL RANDOM(RAND)
242:             1 JR=INT(RAND*M)+1
243:             J=JR
244:             2 A(J)=X(IR(1),J)+FACT*(X(IR(2),J)-X(IR(3),J))
245:             3 J=J+1
246:             IF (J.GT.M) J=1
247:             4 IF (J.EQ.JR) GOTO 10
248:             5 CALL RANDOM(RAND)
249:             IF (PCROS.LE.RAND) GOTO 2
250:             6 A(J)=X(I,J)
251:             7 J=J+1
252:             IF (J.GT.M) J=1
253:             8 IF (J.EQ.JR) GOTO 10
254:             9 GOTO 6
255:             10 CONTINUE
256:         ENDIF
257: C ----- SCHEME 3 -----
258: C ESPECIALLY SUITABLE TO NON-DECOMPOSABLE (NON-SEPERABLE) FUNCTIONS
259: C CROSSOVER SCHEME (NEW) SUGGESTED BY KENNETH PRICE IN HIS
260: C PERSONAL LETTER TO THE AUTHOR (DATED OCTOBER 18, 2006)
261:         IF (NCROSS.GE.2) THEN
262:             CALL RANDOM(RAND)
263:             IF (RAND.LE.PCROS) THEN
264:                 CALL NORMAL(RN)
265:                 DO J=1,M
266:                     A(J)=X(I,J)+(X(IR(1),J)+X(IR(2),J)-2*X(I,J))*RN
267:                 ENDDO
268:             ELSE

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269:         DO J=1,M
270:         A(J)=X(I,J)+(X(IR(1),J)- X(IR(2),J)) ! FACT ASSUMED TO BE 1
271:         ENDDO
272:     ENDIF
273: ENDIF
274: C -----
275:     CALL FUNC(A,M,F) ! EVALUATE THE OFFSPRING
276:     IF(F.LT.FV(I)) THEN ! IF BETTER, REPLACE PARENTS BY THE CHILD
277:     FV(I)=F
278:     DO J=1,M
279:     Y(I,J)=A(J)
280:     ENDDO
281:     ENDIF
282: ENDDO ! I LOOP ENDS
283: DO I=1,N
284: DO J=1,M
285: X(I,J)=Y(I,J) ! NEW GENERATION IS A MIX OF BETTER PARENTS AND
286: C BETTER CHILDREN
287: ENDDO
288: ENDDO
289: IPCOUNT=IPCOUNT+1
290: IF(IPCOUNT.EQ.IPRINT) THEN
291: DO J=1,M
292: A(J)=X(KB,J)
293: ENDDO
294: WRITE(*,*) (X(KB,J),J=1,M), ' FBEST UPTO NOW = ',FBEST
295: WRITE(*,*) 'TOTAL NUMBER OF FUNCTION CALLS = ',NFCALL
296: IF(DABS(FBEST-GBEST).LT.EPS) THEN
297: WRITE(*,*) FTIT
298: WRITE(*,*) 'COMPUTATION OVER'
299: GOTO 999
300: ELSE
301: GBEST=FBEST
302: ENDIF
303: IPCOUNT=0
304: ENDIF
305: C -----
306: 100 ENDDO ! ITERATION ENDS : GO FOR NEXT ITERATION, IF APPLICABLE
307: C -----
308: WRITE(*,*) 'DID NOT CONVERGE. REDUCE EPS OR RAISE ITER OR DO BOTH'
309: WRITE(*,*) 'INCREASE N, PCROS, OR SCALE FACTOR (FACT)'
310: 999 CALL GINI(FV,N,G1)
311: RETURN
312: END
313: C -----
314: SUBROUTINE NORMAL(R)
315: C PROGRAM TO GENERATE N(0,1) FROM RECTANGULAR RANDOM NUMBERS
316: C IT USES BOX-MULLER VARIATE TRANSFORMATION FOR THIS PURPOSE.
317: C -----
318: C ----- BOX-MULLER METHOD BY GEP BOX AND ME MULLER (1958) -----
319: C BOX, G. E. P. AND MULLER, M. E. "A NOTE ON THE GENERATION OF
320: C RANDOM NORMAL DEVIATES." ANN. MATH. STAT. 29, 610-611, 1958.
321: C IF U1 AND U2 ARE UNIFORMLY DISTRIBUTED RANDOM NUMBERS (0,1),
322: C THEN X=[(-2*LN(U1))**.5]*(COS(2*PI*U2) IS N(0,1)
323: C ALSO, X=[(-2*LN(U1))**.5]*(SIN(2*PI*U2) IS N(0,1)
324: C PI = 4*ARCTAN(1.0)= 3.1415926535897932384626433832795
325: C 2*PI = 6.283185307179586476925286766559
326: C -----
327: IMPLICIT DOUBLE PRECISION (A-H,O-Z)
328: COMMON /RNDM/IU,IV
329: INTEGER IU,IV
330: C -----
331: C -----
332: C -----
333: CALL RANDOM(RAND) ! INVOKES RANDOM TO GENERATE UNIFORM RAND [0, 1]
334: U1=RAND ! U1 IS UNIFORMLY DISTRIBUTED [0, 1]
335: CALL RANDOM(RAND) ! INVOKES RANDOM TO GENERATE UNIFORM RAND [0, 1]

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336:      U2=RAND ! U1 IS UNIFORMLY DISTRIBUTED [0, 1]
337:      R=DSQRT(-2.D0*DLOG(U1))
338:      R=R*DCOS(U2*6.283185307179586476925286766559D00)
339: C     R=R*DCOS(U2*6.28318530718D00)
340:      RETURN
341:      END
342: C
343: C     RANDOM NUMBER GENERATOR (UNIFORM BETWEEN 0 AND 1 - BOTH EXCLUSIVE)
344:      SUBROUTINE RANDOM(RAND1)
345:      DOUBLE PRECISION RAND1
346:      COMMON /RNDM/IU,IV
347:      INTEGER IU,IV
348:      RAND=REAL(RAND1)
349:      IV=IU*65539
350:      IF(IV.LT.0) THEN
351:      IV=IV+2147483647+1
352:      ENDIF
353:      RAND=IV
354:      IU=IV
355:      RAND=RAND*0.4656613E-09
356:      RAND1= RAND
357:      RETURN
358:      END
359: C
360: C
361:      SUBROUTINE RPS(M,BST,FMINIM,H0,H1)
362: C     PROGRAM TO FIND GLOBAL MINIMUM BY REPULSIVE PARTICLE SWARM METHOD
363: C     WRITTEN BY SK MISHRA, DEPT. OF ECONOMICS, NEHU, SHILLONG (INDIA)
364: C
365:      PARAMETER (N=100,NN=50,MX=50,NSTEP=11,ITRN=10000,NSIGMA=1,ITOP=3)
366: C     PARAMETER (N=50,NN=25,MX=100,NSTEP=9,ITRN=10000,NSIGMA=1,ITOP=3)
367: C     PARAMETER (N=100,NN=15,MX=100,NSTEP=9,ITRN=10000,NSIGMA=1,ITOP=3)
368: C     IN CERTAIN CASES THE ONE OR THE OTHER SPECIFICATION WORKS BETTER
369: C     DIFFERENT SPECIFICATIONS OF PARAMETERS MAY SUIT DIFFERENT TYPES
370: C     OF FUNCTIONS OR DIMENSIONS - ONE HAS TO DO SOME TRIAL AND ERROR
371: C
372: C     N = POPULATION SIZE. IN MOST OF THE CASES N=30 IS OK. ITS VALUE
373: C     MAY BE INCREASED TO 50 OR 100 TOO. THE PARAMETER NN IS THE SIZE OF
374: C     RANDOMLY CHOSEN NEIGHBOURS. 15 TO 25 (BUT SUFFICIENTLY LESS THAN
375: C     N) IS A GOOD CHOICE. MX IS THE MAXIMAL SIZE OF DECISION VARIABLES.
376: C     IN F(X1, X2, ..., XM) M SHOULD BE LESS THAN OR EQUAL TO MX. ITRN IS
377: C     THE NO. OF ITERATIONS. IT MAY DEPEND ON THE PROBLEM. 200(AT LEAST)
378: C     TO 500 ITERATIONS MAY BE GOOD ENOUGH. BUT FOR FUNCTIONS LIKE
379: C     ROSENBROCKOR GRIEWANK OF LARGE SIZE (SAY M=30) IT IS NEEDED THAT
380: C     ITRN IS LARGE, SAY 5000 OR EVEN 10000.
381: C     SIGMA INTRODUCES PERTURBATION & HELPS THE SEARCH JUMP OUT OF LOCAL
382: C     OPTIMA. FOR EXAMPLE : RASTRIGIN FUNCTION OF DMENSION 30 OR LARGER
383: C     NSTEP DOES LOCAL SEARCH BY TUNNELLING AND WORKS WELL BETWEEN 5 AND
384: C     15, WHICH IS MUCH ON THE HIGHER SIDE.
385: C     ITOP <=1 (RING); ITOP=2 (RING AND RANDOM); ITOP=>3 (RANDOM)
386: C     NSIGMA=0 (NO CHAOTIC PERTURBATION);NSIGMA=1 (CHAOTIC PERTURBATION)
387: C     NOTE THAT NSIGMA=1 NEED NOT ALWAYS WORK BETTER (OR WORSE)
388: C     SUBROUTINE FUNC( ) DEFINES OR CALLS THE FUNCTION TO BE OPTIMIZED.
389:      IMPLICIT DOUBLE PRECISION (A-H,O-Z)
390:      COMMON /RNDM/IU,IV
391:      COMMON /KFF/KF,NFCALL,FTIT
392:      COMMON /XBASE/XBAS
393:      INTEGER IU,IV
394:      CHARACTER *70 FTIT
395:      DIMENSION X(N,MX),V(N,MX),A(MX),VI(MX),XBAS(500,50)
396:      DIMENSION XX(N,MX),F(N),V1(MX),V2(MX),V3(MX),V4(MX),BST(MX)
397: C     A1 A2 AND A3 ARE CONSTANTS AND W IS THE INERTIA WEIGHT.
398: C     OCCASIONALLY, TINKERING WITH THESE VALUES, ESPECIALLY A3, MAY BE
399: C     NEEDED.
400:      DATA A1,A2,A3,W,SIGMA,EPSI /.5D0,.5D0,5.D-04,.5D00,1.D-03,1.D-08/
401: C
402: C     CALL SUBROUTINE FOR CHOOSING FUNCTION (KF) AND ITS DIMENSION (M)

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403: C      CALL FSELECT(KF,M,FTIT)
404: C      -----
405: GGBEST=1.D30 ! TO BE USED FOR TERMINATION CRITERION
406: LCOUNT=0
407: NFCALL=0
408: WRITE(*,*) '4-DIGITS SEED FOR RANDOM NUMBER GENERATION'
409: WRITE(*,*) 'A FOUR-DIGIT POSITIVE ODD INTEGER, SAY, 1171'
410: C      READ(*,*) IU
411: IU=1111 ! COULD BE ANY OTHER 4 OR 5 DIGIT ODD INTEGER
412: FMIN=1.0E30
413: C      GENERATE N-SIZE POPULATION OF M-TUPLE PARAMETERS X(I,J) RANDOMLY
414: DO I=1,N
415:     DO J=1,M
416: C      CALL RANDOM(RAND) !GENERATE X WITHIN
417: C      X(I,J)=(RAND-0.5D00)*2000 ! GENERATE X WITHIN
418: C      WE GENERATE RANDOM(-1000,1000). HERE MULTIPLIER IS 200.
419: C      TINKERING IN SOME CASES MAY BE NEEDED
420: X(I,J)=XBAS(I,J) ! GET X FROM OUTSIDE
421:     ENDDO
422:     F(I)=1.0D30
423: ENDDO
424: C      INITIALISE VELOCITIES V(I) FOR EACH INDIVIDUAL IN THE POPULATION
425: DO I=1,N
426:     DO J=1,M
427:     CALL RANDOM(RAND)
428:     V(I,J)=(RAND-0.5D+00)
429: C      V(I,J)=RAND
430: ENDDO
431: ENDDO
432: DO 100 ITER=1,ITRN
433: C      LET EACH INDIVIDUAL SEARCH FOR THE BEST IN ITS NEIGHBOURHOOD
434:     DO I=1,N
435:         DO J=1,M
436:             A(J)=X(I,J)
437:             VI(J)=V(I,J)
438:             ENDDO
439:             CALL LSRCH(A,M,VI,NSTEP,F,I)
440:             IF(FI.LT.F(I)) THEN
441:                 F(I)=FI
442:                 DO IN=1,M
443:                     BST(IN)=A(IN)
444:                 ENDDO
445: C      F(I) CONTAINS THE LOCAL BEST VALUE OF FUNCTION FOR ITH INDIVIDUAL
446: C      XX(I,J) IS THE M-TUPLE VALUE OF X ASSOCIATED WITH LOCAL BEST F(I)
447:                 DO J=1,M
448:                     XX(I,J)=A(J)
449:                 ENDDO
450:             ENDF
451:         ENDDO
452:     IF(ITER.EQ.1) CALL GINI(F,N,H0)
453: C      NOW LET EVERY INDIVIDUAL RANDOMLY COSULT NN(<<N) COLLEAGUES AND
454: C      FIND THE BEST AMONG THEM
455:     DO I=1,N
456: C      -----
457:     IF(ITOP.GE.3) THEN
458: C      RANDOM TOPOLOGY *****
459: C      CHOOSE NN COLLEAGUES RANDOMLY AND FIND THE BEST AMONG THEM
460:         BEST=1.0D30
461:         DO II=1,NN
462:             CALL RANDOM(RAND)
463:             NF=INT(RAND*N)+1
464:             IF(BEST.GT.F(NF)) THEN
465:                 BEST=F(NF)
466:                 NFBEST=NF
467:             ENDF
468:         ENDDO
469:     ENDF

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470: C-----
471: IF (ITOP.EQ.2) THEN
472: C   RING + RANDOM TOPOLOGY *****
473: C   REQUIRES THAT THE SUBROUTINE NEIGHBOR IS TURNED ALIVE
474:   BEST=1.0D30
475:   CALL NEIGHBOR(I,N,I1,I3)
476:   DO II=1,NN
477:     IF (II.EQ.1) NF=I1
478:     IF (II.EQ.2) NF=I
479:     IF (II.EQ.3) NF=I3
480:     IF (II.GT.3) THEN
481:       CALL RANDOM(RAND)
482:       NF=INT(RAND*N)+1
483:     ENDIF
484:     IF (BEST.GT.F(NF)) THEN
485:       BEST=F(NF)
486:       NFBEST=NF
487:     ENDIF
488:   ENDDO
489: ENDIF
490: C-----
491: IF (ITOP.LE.1) THEN
492: C   RING TOPOLOGY *****
493: C   REQUIRES THAT THE SUBROUTINE NEIGHBOR IS TURNED ALIVE
494:   BEST=1.0D30
495:   CALL NEIGHBOR(I,N,I1,I3)
496:   DO II=1,3
497:     IF (II.NE.I) THEN
498:       IF (II.EQ.1) NF=I1
499:       IF (II.EQ.3) NF=I3
500:       IF (BEST.GT.F(NF)) THEN
501:         BEST=F(NF)
502:         NFBEST=NF
503:       ENDIF
504:     ENDIF
505:   ENDDO
506: ENDIF
507: C-----
508: C   IN THE LIGHT OF HIS OWN AND HIS BEST COLLEAGUES EXPERIENCE, THE
509: C   INDIVIDUAL I WILL MODIFY HIS MOVE AS PER THE FOLLOWING CRITERION
510: C   FIRST, ADJUSTMENT BASED ON ONES OWN EXPERIENCE
511: C   AND OWN BEST EXPERIENCE IN THE PAST (XX(I))
512:   DO J=1,M
513:     CALL RANDOM(RAND)
514:     V1(J)=A1*RAND*(XX(I,J)-X(I,J))
515: C   THEN BASED ON THE OTHER COLLEAGUES BEST EXPERIENCE WITH WEIGHT W
516: C   HERE W IS CALLED AN INERTIA WEIGHT 0.01< W < 0.7
517: C   A2 IS THE CONSTANT NEAR BUT LESS THAN UNITY
518:     CALL RANDOM(RAND)
519:     V2(J)=V(I,J)
520:     IF (F(NFBEST).LT.F(I)) THEN
521:       V2(J)=A2*W*RAND*(XX(NFBEST,J)-X(I,J))
522:     ENDIF
523: C   THEN SOME RANDOMNESS AND A CONSTANT A3 CLOSE TO BUT LESS THAN UNITY
524:     CALL RANDOM(RAND)
525:     RND1=RAND
526:     CALL RANDOM(RAND)
527:     V3(J)=A3*RAND*W*RND1
528: C   V3(J)=A3*RAND*W
529: C   THEN ON PAST VELOCITY WITH INERTIA WEIGHT W
530:     V4(J)=W*V(I,J)
531: C   FINALLY A SUM OF THEM
532:     V(I,J)= V1(J)+V2(J)+V3(J)+V4(J)
533:   ENDDO
534: ENDDO
535: C   CHANGE X
536: DO I=1,N

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537:      DO J=1,M
538:      RANDB=0.D00
539: C -----
540:      IF (NSIGMA.EQ.1) THEN
541:          CALL RANDOM(RAND) ! FOR CHAOTIC PERTURBATION
542:          IF (DABS (RAND-.5D00) .LT. SIGMA) RANDB=RAND-0.5D00
543: C      SIGMA CONDITIONED RANDB INTRODUCES CHAOTIC ELEMENT IN TO LOCATION
544: C      IN SOME CASES THIS PERTURBATION HAS WORKED VERY EFFECTIVELY WITH
545: C      PARAMETER (N=100,NN=15,MX=100,NSTEP=9,ITRN=100000,NSIGMA=1,ITOP=2)
546:      ENDIF
547: C -----
548:      X(I,J)=X(I,J)+V(I,J)*(1.D00+RANDB)
549:      ENDDO
550:      ENDDO
551:      DO I=1,N
552:          IF (F(I) .LT. FMIN) THEN
553:              FMIN=F(I)
554:              II=I
555:              DO J=1,M
556:                  BST(J)=XX(II,J)
557:              ENDDO
558:          ENDIF
559:      ENDDO
560:      IF (LCOUNT.EQ.100) THEN
561:          LCOUNT=0
562:          WRITE (*,*) 'OPTIMAL SOLUTION UPTO THIS (FUNCTION CALLS=',NFCALL,')'
563:          WRITE (*,*) 'X = ', (BST(J),J=1,M), ' MIN F = ',FMIN
564: C      WRITE (*,*) 'NO. OF FUNCTION CALLS = ',NFCALL
565:          IF (DABS (FMIN-GGBEST) .LT. EPSI) THEN
566:              WRITE (*,*) 'COMPUTATION OVER'
567:              FMINIM=FMIN
568:              GOTO 999
569:          ELSE
570:              GGBEST=FMIN
571:          ENDIF
572:      ENDIF
573:      LCOUNT=LCOUNT+1
574: 100 CONTINUE
575:      WRITE (*,*) 'COMPUTATION OVER:',FTIT
576:      FMINIM=FMIN
577: 999 CALL GINI (F,N,H1)
578:      RETURN
579:      END
580: C -----
581:      SUBROUTINE LSRCH (A,M,VI,NSTEP,FI)
582:      IMPLICIT DOUBLE PRECISION (A-H,O-Z)
583:      COMMON /RNDM/IU,IV
584:      INTEGER IU,IV
585:      DIMENSION A(*),B(100),VI(*)
586:      AMN=1.0D30
587:      DO J=1,NSTEP
588:          DO JJ=1,M
589:              B(JJ)=A(JJ)+(J-(NSTEP/2)-1)*VI(JJ)
590:          ENDDO
591:          CALL FUNC (B,M,FI)
592:          IF (FI .LT. AMN) THEN
593:              AMN=FI
594:              DO JJ=1,M
595:                  A(JJ)=B(JJ)
596:              ENDDO
597:          ENDIF
598:      ENDDO
599:      FI=AMN
600:      RETURN
601:      END
602: C -----
603: C      THIS SUBROUTINE IS NEEDED IF THE NEIGHBOURHOOD HAS RING TOPOLOGY

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604: C      EITHER PURE OR HYBRIDIZED
605: C      SUBROUTINE NEIGHBOR(I,N,J,K)
606: C      IF(I-1.GE.1 .AND. I.LT.N) THEN
607: C      J=I-1
608: C      K=I+1
609: C      ELSE
610: C      IF(I-1.LT.1) THEN
611: C      J=N-I+1
612: C      K=I+1
613: C      ENDIF
614: C      IF(I.EQ.N) THEN
615: C      J=I-1
616: C      K=1
617: C      ENDIF
618: C      ENDIF
619: C      RETURN
620: C      END
621: C
622: C      -----
623: C      BARTER ALGORITHM
624: C      -----
625: C      ***** THIS METHOD IS PROPOSED BY SK MISHRA *****
626: C      PROGRAM BY SK MISHRA, DEPT. OF ECONOMICS, NEHU, SHILLONG (INDIA)
627: C      -----
627: C      SUBROUTINE BARTER(M,BEST,FBEST,G0,G1)
628: C      IMPLICIT DOUBLE PRECISION (A-H, O-Z) ! TYPE DECLARATION
629: C      PARAMETER (IPRINT=500, EPS=1.D-08)
630: C      COMMON /RNDM/IU,IV ! RANDOM NUMBER GENERATION (IU = 4-DIGIT SEED)
631: C      COMMON /XBASE/XBAS
632: C      INTEGER IU,IV ! FOR RANDOM NUMBER GENERATION
633: C      COMMON /KFF/KF,NFCALL,FTIT ! FUNCTION CODE,NO. OF CALLS & TITLE
634: C      CHARACTER *70 FTIT ! TITLE OF THE FUNCTION
635: C      -----
636: C      ----- VERY IMPORTANT -----
637: C      FOR THE BARTER METHOD THE DIMENSION M MUST EXCEED UNITY : OR M =>2
638: C      -----
639: C      DIMENSION X(500,50),FV(500),A(50),B(50),BEST(50),XBAS(500,50)
640: C      -----
641: C      ----- SELECT THE FUNCTION TO MINIMIZE AND ITS DIMENSION -----
642: C      CALL FSELECT(KF,M,FTIT)
643: C      SPECIFY OTHER PARAMETERS -----
644: C      WRITE(*,*) 'POPULATION SIZE [N] AND NO. OF ITERATIONS [ITER] ?'
645: C      READ(*,*) N,ITER
646: C      -----
647: C      NBART=0 ! NO. OF TIMES THE BARTER WAS SUCCESSFUL
648: C      NTRY=0 ! NO. OF TIMES ATTEMPT WAS MADE TO BARTER
649: C      N=M*10
650: C      IF(N.LT.100) N=100
651: C      ITER=10000
652: C      WRITE(*,*) 'RANDOM NUMBER SEED ?'
653: C      READ(*,*) IU
654: C      IU=7113 ! COULD BE ANY OTHER 4 OR 5 DIGIT ODD INTEGER
655: C      -----
656: C      NFCALL=0 ! INITIALIZE COUNTER FOR FUNCTION CALLS
657: C      GBEST=1.D30 ! TO BE USED FOR TERMINATION CRITERION
658: C      INITIALIZATION : GENERATE X(N,M) RANDOMLY
659: C      DO I=1,N
660: C      DO J=1,M
661: C      CALL RANDOM(RAND) ! GENERATE INITIAL X WITHIN
662: C      X(I,J)=(RAND-.5D00)*2000 ! GENERATE INITIAL X WITHIN
663: C      RANDOM NUMBERS BETWEEN -RRANGE AND +RRANGE (BOTH EXCLUSIVE)
664: C      X(I,J)=XBAS(I,J) ! : GET X FROM OUTSIDE
665: C      ENDDO
666: C      ENDDO
667: C      WRITE(*,*) 'COMPUTING --- PLEASE WAIT '
668: C      IPCOUNT=0
669: C      DO 100 ITR=1,ITER ! ITERATION BEGINS
670: C

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671: C      EVALUATE ALL X FOR THE GIVEN FUNCTION
672: DO I=1,N
673:     DO J=1,M
674:         A(J)=X(I,J)
675:     ENDDO
676: CALL FUNC(A,M,FA)
677: FV(I)=FA
678: C      -----
679:     CALL SEARCH(A,M,FI)
680: C      STORE FUNCTION VALUES IN FV VECTOR
681:     IF(FI.LT.FV(I)) THEN
682:         DO J=1,M
683:             X(I,J)=A(J)
684:         ENDDO
685:         FV(I)=FI
686:     ENDIF
687: ENDDO
688: IF(ITR.EQ.1) CALL GINI(FV,N,G0)
689: C      -----
690: DO I=1,N
691:     NTRY=NTRY+1
692: C      CHOOSE IB TH INDIVIDUAL RANDOMLY
693: CALL RANDOM(RAND)
694: IB=INT(RAND*N)+1 !THE RANDOM INDIVIDUAL
695: C      IB=2*M+1
696: C      STORE ITH IN A AND RANDOMLY SELECTED INDIVIDUAL IN B
697:     DO J=1,M
698:         A(J)=X(I,J)
699:         B(J)=X(IB,J) ! OF THE INDIVIDUAL RANDOMLY SELECTED
700:     ENDDO
701: C      CHOSE AN INDEX BETWEEN 1 AND M RANDOMLY
702:     CALL RANDOM(RAND)
703:     JA=INT(RAND*M)+1
704: C      CHOOSE ANOTHER INDEX RANDOMLY : MUST BE DIFFERENT FROM JA
705: 1     CALL RANDOM(RAND)
706:     JB=INT(RAND*M)+1
707:     IF(JA.EQ.JB) GOTO 1
708: C      EXCHANGE A(JA) WITH B(JB)
709:     TEMP1=A(JA)
710:     TEMP2=B(JB)
711:     CALL NORMAL(RN) ! OBTAIN STANDARD NORMAL RANDOM NUMBER
712:     A(JB)=A(JB)+RN*TEMP2
713:     B(JB)=B(JB)-RN*TEMP2
714:     A(JA)=A(JA)-RN*TEMP1
715:     B(JA)=B(JA)+RN*TEMP1
716: C      EVALUATE A AND B VECTORS
717:     CALL FUNC(A,M,FA)
718:     CALL FUNC(B,M,FB)
719: C      CHECK IF FA < FV(I) AND FB < FV(IB)
720:     IF(FA.LT.FV(I) .AND. FB.LT.FV(IB)) THEN
721:         NBART=NBART+1
722:         FV(I)=FA
723:         FV(IB)=FB
724:         DO J=1,M
725:             X(I,J)=A(J)
726:             X(IB,J)=B(J)
727:         ENDDO
728:     ENDIF
729: ENDDO
730: C      -----
731: C      FIND THE BEST
732: FBEST=1.D30
733: DO I=1,N
734:     IF(FV(I).LT.FBEST) THEN
735:         FBEST=FV(I)
736:         KB=I
737:     ENDIF

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738:      ENDDO
739:      DO J=1,M
740:      BEST(J)=X(KB,J)
741:      ENDDO
742: C -----
743:      IPCOUNT=IPCOUNT+1
744:      IF (IPCOUNT.EQ.IPRINT) THEN
745:      WRITE (*,*) (BEST(J),J=1,M), ' FBEST UPTO NOW = ',FBEST
746:      WRITE (*,*) 'TOTAL NUMBER OF FUNCTION CALLS = ',NFCALL
747:      IF (DABS (FBEST-GBEST) .LT.EPS) THEN
748:      WRITE (*,*) FTIT
749:      WRITE (*,*) 'COMPUTATION OVER'
750:      GOTO 999
751:      ELSE
752:      GBEST=FBEST
753:      ENDIF
754:      IPCOUNT=0
755:      ENDIF
756: C -----
757: 100 ENDDO ! ITERATION ENDS : GO FOR NEXT ITERATION, IF APPLICABLE
758: C -----
759:      WRITE (*,*) 'DID NOT CONVERGE. REDUCE EPS -- MAY MAKE IT ZERO --'
760:      WRITE (*,*) 'RAISE ITER OR DO BOTH OR INCREASE N, POPULATION SIZE'
761: 999 CALL GINI (FV,N,G1)
762:      PSUCCESS=NBART/DFLOAT (NTRY) *100.0
763:      WRITE (*,*) 'NO. OF TIMES AN ATTEMPT TO BARTER WAS MADE = ', NTRY
764:      WRITE (*,*) 'NO. OF TIMES BARTER WAS SUCCESSFUL = ', NBART
765:      WRITE (*,*) 'PERCENTAGE SUCCESS OF BARTER ATTEMPTS = ', PSUCCESS
766:      RETURN
767:      END
768: C -----
769:      SUBROUTINE SEARCH (A,M,FI)
770:      IMPLICIT DOUBLE PRECISION (A-H,O-Z)
771:      COMMON /RNDM/IU,IV
772:      INTEGER IU,IV
773:      DIMENSION A (*),B (100)
774:      NSTEP=11
775:      AMN=1.0D30
776:      DO J=1,NSTEP
777:      DO JJ=1,M
778:      CALL RANDOM (RAND)
779:      B (JJ)=A (JJ) + (J- (NSTEP/2) -1) *RAND*0.0001D00
780:      ENDDO
781:      CALL FUNC (B,M,FI)
782:      IF (FI.LT.AMN) THEN
783:      AMN=FI
784:      DO JJ=1,M
785:      A (JJ)=B (JJ)
786:      ENDDO
787:      ENDIF
788:      ENDDO
789:      FI=AMN
790:      RETURN
791:      END
792: C -----
793:      SUBROUTINE GINI (F,N,G)
794:      PARAMETER (K=1) !K=1 GINI COEFFICIENT; K=2 COEFFICIENT OF VARIATION
795: C THIS PROGRAM COMPUTES MEASURE OF INEQUALITY
796: C IF K =1 GET THE GINI COEFFICIENT. IF K=2 GET COEFF OF VARIATIONE
797:      IMPLICIT DOUBLE PRECISION (A-H,O-Z)
798:      DIMENSION F (*)
799:      S=0.D0
800:      DO I=1,N
801:      S=S+F (I)
802:      ENDDO
803:      S=S/N
804:      H=0.D00

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805:      DO I=1,N-1
806:      DO J=I+1,N
807:      H=H+(DABS(F(I)-F(J)))**K
808:      ENDDO
809:      ENDDO
810:      H=(H/(N**2))**(1.D0/K) ! FOR K=1 H IS MEAN DEVIATION;
811: C      FOR K=2 H IS STANDARD DEVIATION
812:      WRITE(*,*)'MEASURES OF DISPERSION AND CENTRAL TENDENCY = ',G,S
813:      G=DEXP(-H) ! G IS THE MEASURE OF EQUALITY (NOT GINI OR CV)
814: C      G=H/DABS(S) !IF S NOT ZERO, K=1 THEN G=GINI, K=2 G=COEFF VARIATION
815:      RETURN
816:      END
817: C
818:      SUBROUTINE FSELECT(KF,M,FTIT)
819: C      THE PROGRAM REQUIRES INPUTS FROM THE USER ON THE FOLLOWING -----
820: C      (1) FUNCTION CODE (KF), (2) NO. OF VARIABLES IN THE FUNCTION (M);
821:      CHARACTER *70 TIT(100),FTIT
822:      WRITE(*,*)'-----'
823:      DATA TIT(1)/'KF=1 NEW FUNCTION(N#1) 2-VARIABLES M=2'/
824:      DATA TIT(2)/'KF=2 NEW FUNCTION(N#2) 2-VARIABLES M=2'/
825:      DATA TIT(3)/'KF=3 NEW FUNCTION(N#3) 2-VARIABLES M=2'/
826:      DATA TIT(4)/'KF=4 NEW FUNCTION(N#4) 2-VARIABLES M=2'/
827:      DATA TIT(5)/'KF=5 NEW QUINTIC FUNCTION M-VARIABLES M=?'/
828:      DATA TIT(6)/'KF=6 NEW NEEDLE-EYE FUNCTION (N#6) M-VARIABLES M=?'/
829:      DATA TIT(7)/'KF=7 NEW ZERO-SUM FUNCTION (N#7) M-VARIABLES M=?'/
830:      DATA TIT(8)/'KF=8 CORANA FUNCTION 4-VARIABLES M=4'/
831:      DATA TIT(9)/'KF=9 MODIFIED RCOS FUNCTION 2-VARIABLES M=2'/
832:      DATA TIT(10)/'KF=10 FREUDENSTEIN ROTH FUNCTION 2-VARIABLES M=2'/
833:      DATA TIT(11)/'KF=11 ANNS XOR FUNCTION 9-VARIABLES M=9'/
834:      DATA TIT(12)/'KF=12 PERM FUNCTION #1 (SET BETA) 4-VARIABLES M=4'/
835:      DATA TIT(13)/'KF=13 PERM FUNCTION #2 (SET BETA) M-VARIABLES M=?'/
836:      DATA TIT(14)/'KF=14 POWER-SUM FUNCTION 4-VARIABLES M=4'/
837:      DATA TIT(15)/'KF=15 GOLDSTEIN PRICE FUNCTION 2-VARIABLES M=2'/
838:      DATA TIT(16)/'KF=16 BUKIN 6TH FUNCTION 2-VARIABLES M=2'/
839:      DATA TIT(17)/'KF=17 NEW FUNCTION (N#8) 2-VARIABLES M=2'/
840:      DATA TIT(18)/'KF=18 DEFL CORRUG SPRING FUNCTION M-VARIABLES M=?'/
841:      DATA TIT(19)/'KF=19 NEW FACTORIAL FUNCTION M-VARIABLES M=?'/
842:      DATA TIT(20)/'KF=20 NEW DECANOMIAL FUNCTION 2-VARIABLES M=2'/
843:      DATA TIT(21)/'KF=21 JUDGE FUNCTION 2-VARIABLES M=2'/
844:      DATA TIT(22)/'KF=22 NEW DODECAL FUNCTION 3-VARIABLES M=3'/
845:      DATA TIT(23)/'KF=23 NEW SUM-EQ-PROD FUNCTION 2-VARIABLES M=2'/
846:      DATA TIT(24)/'KF=24 NEW AM-EQ-GM FUNCTION M-VARIABLES M=?'/
847:      DATA TIT(25)/'KF=25 YAO-LIU FUNCTION#2 M-VARIABLES M=?'/
848:      DATA TIT(26)/'KF=26 YAO-LIU FUNCTION#3 M-VARIABLES M=?'/
849:      DATA TIT(27)/'KF=27 YAO-LIU FUNCTION#4 M-VARIABLES M=?'/
850:      DATA TIT(28)/'KF=28 YAO-LIU FUNCTION#6 M-VARIABLES M=?'/
851:      DATA TIT(29)/'KF=29 YAO-LIU FUNCTION#7 M-VARIABLES M=?'/
852:      DATA TIT(30)/'KF=30 YAO-LIU FUNCTION#12 M-VARIABLES M=?'/
853:      DATA TIT(31)/'KF=31 YAO-LIU FUNCTION#13 M-VARIABLES M=?'/
854:      DATA TIT(32)/'KF=32 YAO-LIU FUNCTION#14 2-VARIABLES M=2'/
855:      DATA TIT(33)/'KF=33 YAO-LIU FUNCTION#15 4-VARIABLES M=4'/
856:      DATA TIT(34)/'KF=34 WOOD FUNCTION : 4-VARIABLES M=4'/
857:      DATA TIT(35)/'KF=35 FENTON-EASON FUNCTION : 2-VARIABLES M=2'/
858:      DATA TIT(36)/'KF=36 HOUGEN FUNCTION : 5-VARIABLES M=5'/
859:      DATA TIT(37)/'KF=37 GIUNTA FUNCTION : 2-VARIABLES M=2'/
860:      DATA TIT(38)/'KF=38 EGGHOLDER FUNCTION : M-VARIABLES M=?'/
861:      DATA TIT(39)/'KF=39 TRID FUNCTION : M-VARIABLES M=?'/
862:      DATA TIT(40)/'KF=40 GRIEWANK FUNCTION : M-VARIABLES M=?'/
863:      DATA TIT(41)/'KF=41 WEIERSTRASS FUNCTION : M-VARIABLES M=?'/
864:      DATA TIT(42)/'KF=42 LEVY-3 FUNCTION : 2-VARIABLES M=2'/
865:      DATA TIT(43)/'KF=43 LEVY-5 FUNCTION : 2-VARIABLES M=2'/
866:      DATA TIT(44)/'KF=44 LEVY-8 FUNCTION : 3-VARIABLES M=3'/
867:      DATA TIT(45)/'KF=45 RASTRIGIN FUNCTION : M-VARIABLES M=?'/
868:      DATA TIT(46)/'KF=46 ACKLEY FUNCTION : M-VARIABLES M=?'/
869:      DATA TIT(47)/'KF=47 MICHALEWICZ FUNCTION : M-VARIABLES M=?'/
870:      DATA TIT(48)/'KF=48 SCHWEFEL FUNCTION : M-VARIABLES M=?'/
871:      DATA TIT(49)/'KF=49 SHUBERT FUNCTION : 2-VARIABLES M=2'/

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872:      DATA TIT(50) / 'KF=50 DIXON-PRICE FUNCTION : M-VARIABLES M=?' /
873:      DATA TIT(51) / 'KF=51 SHEKEL FUNCTION : 4-VARIABLES M=4' /
874:      DATA TIT(52) / 'KF=52 PAVIANI FUNCTION : 10-VARIABLES M=10' /
875:      DATA TIT(53) / 'KF=53 BRANIN FUNCTION#1 : 2-VARIABLES M=2' /
876:      DATA TIT(54) / 'KF=54 BRANIN FUNCTION#2 : 2-VARIABLES M=2' /
877:      DATA TIT(55) / 'KF=55 BOHACHEVSKY FUNCTION#1 : 2-VARIABLES M=2' /
878:      DATA TIT(56) / 'KF=56 BOHACHEVSKY FUNCTION#2 : 2-VARIABLES M=2' /
879:      DATA TIT(57) / 'KF=57 BOHACHEVSKY FUNCTION#3 : 2-VARIABLES M=2' /
880:      DATA TIT(58) / 'KF=58 EASOM FUNCTION : 2-VARIABLES M=2' /
881:      DATA TIT(59) / 'KF=59 ROSENBROCK FUNCTION : M-VARIABLES M=?' /
882:      DATA TIT(60) / 'KF=60 CROSS-LEGGED TABLE FUNCTION:2-VARIABLES M=2' /
883:      DATA TIT(61) / 'KF=61 CROSS FUNCTION : 2-VARIABLES M=2' /
884:      DATA TIT(62) / 'KF=62 CROSS-IN-TRAY FUNCTION : 2-VARIABLES M=2' /
885:      DATA TIT(63) / 'KF=63 CROWNED CROSS FUNCTION : 2-VARIABLES M=2' /
886:      DATA TIT(64) / 'KF=64 TT-HOLDER FUNCTION : 2-VARIABLES M=2' /
887:      DATA TIT(65) / 'KF=65 HOLDER-TABLE FUNCTION : 2-VARIABLES M=2' /
888:      DATA TIT(66) / 'KF=66 CARROM-TABLE FUNCTION : 2-VARIABLES M=2' /
889:      DATA TIT(67) / 'KF=67 PENHOLDER FUNCTION : 2-VARIABLES M=2' /
890:      DATA TIT(68) / 'KF=68 BIRD FUNCTION : 2-VARIABLES M=2' /
891:      DATA TIT(69) / 'KF=69 CHICHINADZE FUNCTION : 2-VARIABLES M=2' /
892:      DATA TIT(70) / 'KF=70 MCCORMICK FUNCTION : 2-VARIABLES M=2' /
893:      DATA TIT(71) / 'KF=71 GLANKWAHMDEE FUNCTION : 5-VARIABLES M=5' /
894:      DATA TIT(72) / 'KF=72 FLETCHER-POWELL FUNCTION : M-VARIABLES M=?' /
895:      DATA TIT(73) / 'KF=73 POWELL FUNCTION: M-VARIABLES M (MULT OF 4)=?' /
896:      DATA TIT(74) / 'KF=74 HARTMANN FUNCTION: 3-VARIABLES M=3' /
897:      DATA TIT(75) / 'KF=75 COLVILLE FUNCTION: 4-VARIABLES M=4' /
898:      DATA TIT(76) / 'KF=76 HIMMELBLAU FUNCTION: 2-VARIABLES M=2' /
899:      DATA TIT(77) / 'KF=77 BEALE FUNCTION: 2-VARIABLES M=2' /
900:      DATA TIT(78) / 'KF=78 BOOTH FUNCTION: 2-VARIABLES M=2' /
901:      DATA TIT(79) / 'KF=79 HUMP FUNCTION: 2-VARIABLES M=2' /
902:      DATA TIT(80) / 'KF=80 MATYAS FUNCTION: 2-VARIABLES M=2' /
903:      DATA TIT(81) / 'KF=81 MISHRA_1 FUNCTION: M-VARIABLES M=?' /
904:      DATA TIT(82) / 'KF=82 MISHRA_2 FUNCTION: M-VARIABLES M=?' /
905:      DATA TIT(83) / 'KF=83 ZAKHAROV FUNCTION: M-VARIABLES M=?' /
906:      DATA TIT(84) / 'KF=84 MULTIMOD FUNCTION: 2-VARIABLES M=2' /
907:      DATA TIT(85) / 'KF=85 NONLINEAR FUNCTION: M-VARIABLES M=?' /
908:      DATA TIT(86) / 'KF=86 QUADRATIC FUNCTION: 2-VARIABLES M=2' /
909:      DATA TIT(87) / 'KF=87 TRIGON FUNCTION: M-VARIABLES M=?' /
910:      DATA TIT(88) / 'KF=88 COMPOUND FUNCTION: 4-VARIABLES M=4' /
911: C -----
912:      DO I=1, 88
913:      WRITE (*, *) TIT(I)
914:      ENDDO
915:      WRITE (*, *) '-----'
916:      WRITE (*, *) 'FUNCTION CODE [KF] AND NO. OF VARIABLES [M] ?'
917:      READ (*, *) KF, M
918:      FTIT=TIT(KF) ! STORE THE NAME OF THE CHOSEN FUNCTION IN FTIT
919:      RETURN
920:      END
921: C -----
922:      SUBROUTINE FUNC(X, M, F)
923: C TEST FUNCTIONS FOR GLOBAL OPTIMIZATION PROGRAM
924:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
925:      COMMON /RNDM/IU, IV
926:      COMMON /KFF/KF, NFCALL, FTIT
927:      INTEGER IU, IV
928:      DIMENSION X(*)
929:      CHARACTER *70 FTIT
930:      PI=4.D+00*DATAN(1.D+00) ! DEFINING THE VALUE OF PI
931:      NFCALL=NFCALL+1 ! INCREMENT TO NUMBER OF FUNCTION CALLS
932: C KF IS THE CODE OF THE TEST FUNCTION
933: C -----
934:      IF (KF.EQ.1) THEN
935: C FUNCTION #1 MIN AT -0.18467 APPROX AT (-8.4666, -10) APPROX
936:      F=0.D00
937:      DO I=1, M
938:      IF (DABS(X(I)) .GT. 10.D00) THEN

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939:      CALL RANDOM(RAND)
940:      X(I)=(RAND-0.5D00)*20
941:      ENDIF
942:      ENDDO
943:      F=DABS(DCOS(DSQRT(DABS(X(1)**2+X(2)))))**0.5 +0.01*X(1)+.01*X(2)
944:      RETURN
945:      ENDIF
946: C
947:      IF(KF.EQ.2) THEN
948: C      FUNCTION #2 MIN = -0.199409 APPROX AT (-9.94112, -10) APPROX
949:      F=0.D00
950:      DO I=1,M
951:      IF(DABS(X(I)).GT.10.D00) THEN
952:      CALL RANDOM(RAND)
953:      X(I)=(RAND-0.5D00)*20
954:      ENDIF
955:      ENDDO
956:      F=DABS(DSIN(DSQRT(DABS(X(1)**2+X(2)))))**0.5 +0.01*X(1)+.01*X(2)
957:      RETURN
958:      ENDIF
959: C
960:      IF(KF.EQ.3) THEN
961: C      FUNCTION #3 MIN = -1.01983 APPROX AT (-1.98682, -10.00000) APPROX
962:      F=0.D00
963:      DO I=1,M
964:      IF(DABS(X(I)).GT.10.D00) THEN
965:      CALL RANDOM(RAND)
966:      X(I)=(RAND-0.5D00)*20
967:      ENDIF
968:      ENDDO
969:      F1=DSIN((DCOS(X(1))+DCOS(X(2)))**2)**2
970:      F2=DCOS((DSIN(X(1))+DSIN(X(2)))**2)**2
971:      F=(F1+F2+X(1))**2 ! IS MULTIMODAL
972:      F=F+ 0.01*X(1)+0.1*X(2) ! MAKES UNIMODAL
973:      RETURN
974:      ENDIF
975: C
976:      IF(KF.EQ.4) THEN
977: C      FUNCTION #4 MIN = -2.28395 APPROX AT (2.88631, 1.82326) APPROX
978:      F=0.D00
979:      DO I=1,M
980:      IF(DABS(X(I)).GT.10.D00) THEN
981:      CALL RANDOM(RAND)
982:      X(I)=(RAND-0.5D00)*20
983:      ENDIF
984:      ENDDO
985:      F1=DSIN((DCOS(X(1))+DCOS(X(2)))**2)**2
986:      F2=DCOS((DSIN(X(1))+DSIN(X(2)))**2)**2
987:      F3=-DLOG((F1-F2+X(1))**2)
988:      F=F3+0.1D00*(X(1)-1.D00)**2+0.1D00*(X(2)-1.D00)**2
989:      RETURN
990:      ENDIF
991: C
992:      IF(KF.EQ.5) THEN
993: C      QUINTIC FUNCTION:GLOBAL MINIMA,EXTREMELY DIFFICULT TO OPTIMIZE
994: C      MIN VALUE = 0 AT PERMUTATION OF (2, 2,..., 2, -1, -1, ..., -1,
995: C      -0.402627941) GIVES MIN F = 0.
996:      F=0.D00
997:      DO I=1,M
998:      IF(DABS(X(I)).GT.10.D00) THEN
999:      CALL RANDOM(RAND)
1000:      X(I)=(RAND-0.5D00)*20
1001:      ENDIF
1002:      ENDDO
1003:      CALL QUINTIC(M,F,X)
1004:      RETURN
1005:      ENDIF

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1006: C -----
1007: IF (KF.EQ.6) THEN
1008: C NEEDLE-EYE FUNCTION M=>1;
1009: C MIN = 1 IF ALL ABS(X) ARE SMALLER THAN THE EYE
1010: C SMALLER THE VALUE OF ZZ, MORE DIFFICULT TO ENTER THE EYE
1011: C LARGER THE VALUE OF M, MORE DIFFICULT TO FIND THE OPTIMUM
1012: F=0.D00
1013: EYE=0.000001D00
1014: FP=0.D00
1015: DO I=1,M
1016: IF (DABS(X(I)).GT.EYE) THEN
1017: FP=1.D00
1018: F=F+100.D00+DABS(X(I))
1019: ELSE
1020: F=F+1.D00
1021: ENDIF
1022: ENDDO
1023: IF (FP.EQ.0.D00) F=F/M
1024: RETURN
1025: ENDIF
1026: C -----
1027: IF (KF.EQ.7) THEN
1028: C ZERO SUM FUNCTION : MIN = 0 AT SUM(X(I))=0
1029: F=0.D00
1030: DO I=1,M
1031: IF (DABS(X(I)).GT.10.D00) THEN
1032: CALL RANDOM(RAND)
1033: X(I)=(RAND-0.5D00)*20
1034: ENDIF
1035: ENDDO
1036: SUM=0.D00
1037: DO I=1,M
1038: SUM=SUM+X(I)
1039: ENDDO
1040: IF (SUM.NE.0.D00) F=1.D00+(10000*DABS(SUM))**0.5
1041: RETURN
1042: ENDIF
1043: C -----
1044: IF (KF.EQ.8) THEN
1045: C CORANA FUNCTION : MIN = 0 AT (0, 0, 0, 0) APPROX
1046: F=0.D00
1047: DO I=1,M
1048: IF (DABS(X(I)).GT.1000.D00) THEN
1049: CALL RANDOM(RAND)
1050: X(I)=(RAND-0.5D00)*2000
1051: ENDIF
1052: ENDDO
1053: DO J=1,M
1054: IF (J.EQ.1) DJ=1.D00
1055: IF (J.EQ.2) DJ=1000.D00
1056: IF (J.EQ.3) DJ=10.D00
1057: IF (J.EQ.4) DJ=100.D00
1058: ISGNXJ=1
1059: IF (X(J).LT.0.D00) ISGNXJ=-1
1060: ZJ=(DABS(X(J)/0.2D00)+0.49999)*ISGNXJ*0.2D00
1061: ISGNZJ=1
1062: IF (ZJ.LT.0.D00) ISGNZJ=-1
1063: IF (DABS(X(J)-ZJ).LT.0.05D00) THEN
1064: F=F+0.15D00*(ZJ-0.05D00*ISGNZJ)**2 * DJ
1065: ELSE
1066: F=F+DJ*X(J)**2
1067: ENDIF
1068: ENDDO
1069: RETURN
1070: ENDIF
1071: C -----
1072: IF (KF.EQ.9) THEN

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1073: C      MODIFIED RCOS FUNCTION MIN=-0.179891 AT (-3.196989, 12.52626) APPRX
1074: F=0.D00
1075: IF (X(1) .LT. -5.D00 .OR. X(1) .GT. 10.D00) THEN
1076: CALL RANDOM(RAND)
1077: X(1)=RAND*15.D00 -5.D00
1078: ENDF
1079: IF (X(2) .LT. 0.D00 .OR. X(2) .GT. 15.D00) THEN
1080: CALL RANDOM(RAND)
1081: X(2)=RAND*15.D00
1082: ENDF
1083: CA=1.D00
1084: CB=5.1/(4*PI**2)
1085: CC=5.D00/PI
1086: CD=6.D00
1087: CE=10.D00
1088: CF=1.0/(8*PI)
1089: F1=CA*(X(2)-CB*X(1)**2+CC*X(1)-CD)**2
1090: F2=CE*(1.D00-CF)*DCOS(X(1))*DCOS(X(2))
1091: F3=DLOG(X(1)**2+X(2)**2+1.D00)
1092: F=-1.0/(F1+F2+F3+CE)
1093: RETURN
1094: ENDF
-----
1095: C
1096: IF (KF.EQ.10) THEN
1097: C      FREUDENSTEIN ROTH FUNCTION : MIN = 0 AT (5, 4)
1098: F=0.D00
1099: DO I=1,M
1100: IF (DABS(X(I)) .GT. 10.D00) THEN
1101: CALL RANDOM(RAND)
1102: X(I)=(RAND-0.5D00)*20
1103: ENDF
1104: ENDDO
1105: F1=(-13.D00+X(1)+((5.D00-X(2))*X(2)-2)*X(2))**2
1106: F2=(-29.D00+X(1)+((X(2)+1.D00)*X(2)-14.D00)*X(2))**2
1107: F=F1+F2
1108: RETURN
1109: ENDF
-----
1110: C
1111: IF (KF.EQ.11) THEN
1112: C      ANNS XOR FUNCTION (PARSOPOULOS, KE, PLAGIANAKOS, VP, MAGOULAS, GD
1113: C      AND VRAHATIS, MN "STRETCHING TECHNIQUE FOR OBTAINING GLOBAL
1114: C      MINIMIZERS THROUGH PARTICLE SWARM OPTIMIZATION")
1115: C      MIN=0.9597588 FOR X=(1, -1, 1, -1, -1, 1, 1, -1, 0.421134) APPROX
1116: C      OBTAINED BY DIFFERENTIAL EVOLUTION PROGRAM
1117: F=0.D00
1118: DO I=1,M
1119: IF (DABS(X(I)) .GT. 1.D00) THEN
1120: CALL RANDOM(RAND)
1121: X(I)=(RAND-0.5D00)*2
1122: ENDF
1123: ENDDO
1124: F11=X(7)/(1.D00+DEXP(-X(1)-X(2)-X(5)))
1125: F12=X(8)/(1.D00+DEXP(-X(3)-X(4)-X(6)))
1126: F1=(1.D00+DEXP(-F11-F12-X(9)))**(-2)
1127: F21=X(7)/(1.D00+DEXP(-X(5)))
1128: F22=X(8)/(1.D00+DEXP(-X(6)))
1129: F2=(1.D00+DEXP(-F21-F22-X(9)))**(-2)
1130: F31=X(7)/(1.D00+DEXP(-X(1)-X(5)))
1131: F32=X(8)/(1.D00+DEXP(-X(3)-X(6)))
1132: F3=(1.D00-(1.D00+DEXP(-F31-F32-X(9)))**(-1))**2
1133: F41=X(7)/(1.D00+DEXP(-X(2)-X(5)))
1134: F42=X(8)/(1.D00+DEXP(-X(4)-X(6)))
1135: F4=(1.D00-(1.D00+DEXP(-F41-F42-X(9)))**(-1))**2
1136: F=F1+F2+F3+F4
1137: RETURN
1138: ENDF
-----
1139: C

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1140:      IF (KF .EQ. 12) THEN
1141: C      PERM FUNCTION #1 MIN = 0 AT (1, 2, 3, 4)
1142: C      BETA => 0. CHANGE IF NEEDED. SMALLER BETA RAISES DIFFICULTY
1143: C      FOR BETA=0, EVERY PERMUTED SOLUTION IS A GLOBAL MINIMUM
1144:      BETA=50.D00
1145:      F=0.D00
1146:      DO I=1,M
1147:      IF (DABS(X(I)) .GT. M) THEN
1148:      CALL RANDOM(RAND)
1149:      X(I) = (RAND-0.5D00) * 2 * M
1150:      ENDIF
1151:      ENDDO
1152:      DO K=1,M
1153:      SUM=0.D00
1154:      DO I=1,M
1155:      SUM=SUM+ (I**K+BETA) * ((X(I)/I)**K-1.D00)
1156:      ENDDO
1157:      F=F+SUM**2
1158:      ENDDO
1159:      RETURN
1160:      ENDIF
1161: C      -----
1162:      IF (KF .EQ. 13) THEN
1163: C      PERM FUNCTION #2 MIN = 0 AT (1/1, 1/2, 1/3, 1/4, ..., 1/M)
1164: C      BETA => 0. CHANGE IF NEEDED. SMALLER BETA RAISES DIFFICULTY
1165: C      FOR BETA=0, EVERY PERMUTED SOLUTION IS A GLOBAL MINIMUM
1166:      BETA=10.D00
1167:      DO I=1,M
1168:      IF (DABS(X(I)) .GT. 1.D00) THEN
1169:      CALL RANDOM(RAND)
1170:      X(I) = (RAND-.5D00) * 2
1171:      ENDIF
1172:      SGN=X(I)/DABS(X(I))
1173:      ENDDO
1174:      F=0.D00
1175:      DO K=1,M
1176:      SUM=0.D00
1177:      DO I=1,M
1178:      SUM=SUM+ (I+BETA) * (X(I)**K- (1.D00/I)**K)
1179:      ENDDO
1180:      F=F+SUM**2
1181:      ENDDO
1182:      RETURN
1183:      ENDIF
1184: C      -----
1185:      IF (KF .EQ. 14) THEN
1186: C      POWER SUM FUNCTION; MIN = 0 AT PERM(1,2,2,3) FOR B=(8,18,44,114)
1187: C      0 =< X <=4
1188:      F=0.D00
1189:      DO I=1,M
1190: C      ANY PERMUTATION OF (1,2,2,3) WILL GIVE MIN = ZERO
1191:      IF (X(I) .LT. 0.D00 .OR. X(I) .GT. 4.D00) THEN
1192:      CALL RANDOM(RAND)
1193:      X(I) = RAND * 4
1194:      ENDIF
1195:      ENDDO
1196:      DO K=1,M
1197:      SUM=0.D00
1198:      DO I=1,M
1199:      SUM=SUM+X(I)**K
1200:      ENDDO
1201:      IF (K .EQ. 1) B=8.D00
1202:      IF (K .EQ. 2) B=18.D00
1203:      IF (K .EQ. 3) B=44.D00
1204:      IF (K .EQ. 4) B=114.D00
1205:      F=F+ (SUM-B)**2
1206:      ENDDO

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1207:      RETURN
1208:      ENDIF
1209: C -----
1210:      IF (KF.EQ.15) THEN
1211: C      GOLDSTEIN PRICE FUNCTION : MIN VALUE = 3 AT (0, -1)
1212:      F=0.D00
1213:      DO I=1,M
1214:      IF (DABS(X(I)).GT.10.D00) THEN
1215:      CALL RANDOM(RAND)
1216:      X(I)=(RAND-.5D00)*20
1217:      ENDIF
1218:      ENDDO
1219:      F11=(X(1)+X(2)+1.D00)**2
1220:      F12=(19.D00-14*X(1)+3*X(1)**2-14*X(2)+6*X(1)*X(2)+3*X(2)**2)
1221:      F1=1.00+F11*F12
1222:      F21=(2*X(1)-3*X(2))**2
1223:      F22=(18.D00-32*X(1)+12*X(1)**2+48*X(2)-36*X(1)*X(2)+27*X(2)**2)
1224:      F2=30.D00+F21*F22
1225:      F=(F1*F2)
1226:      RETURN
1227:      ENDIF
1228: C -----
1229:      IF (KF.EQ.16) THEN
1230: C      BUKIN'S 6TH FUNCTION MIN = 0 FOR (-10, 1)
1231: C      -15. LE. X(1) .LE. -5 AND -3 .LE. X(2) .LE. 3
1232:      IF (X(1).LT.-15.D00 .OR. X(1).GT.-5.D00) THEN
1233:      CALL RANDOM(RAND)
1234:      X(1)=- (RAND*10+5.D00)
1235:      ENDIF
1236:      IF (DABS(X(2)).GT.3.D00) THEN
1237:      CALL RANDOM(RAND)
1238:      X(2)=(RAND-.5D00)*6
1239:      ENDIF
1240:      F=100.D0*DSQRT(DABS(X(2)-0.01D0*X(1)**2))+0.01D0*DABS(X(1)+10.D0)
1241:      RETURN
1242:      ENDIF
1243: C -----
1244:      IF (KF.EQ.17) THEN
1245: C      NEW N#8 FUNCTION (MULTIPLE GLOBAL MINIMA)
1246: C      MIN VALUE = -1 AT (AROUND .7 AROUND, 0.785 APPROX)
1247:      F=0.D00
1248:      DO I=1,M
1249:      IF (X(I).LT.0.5D00 .OR. X(I).GT.1.D00) THEN
1250:      CALL RANDOM(RAND)
1251:      X(I)=RAND/2.D00
1252:      ENDIF
1253:      ENDDO
1254:      F=-DEXP(-DABS(DLOG(.001D00+DABS((DSIN(X(1)+X(2))+DSIN(X(1)-X(2)))+
1255:      & (DCOS(X(1)+X(2))*DCOS(X(1)-X(2))+.001)**2))+
1256:      & .01D00*(X(2)-X(1))**2)))
1257:      RETURN
1258:      ENDIF
1259: C -----
1260:      IF (KF.EQ.18) THEN
1261: C      DEFLECTED CORRUGATED SPRING FUNCTION
1262: C      MIN VALUE = -1 AT (5, 5, ..., 5) FOR ANY K AND ALPHA=5; M VARIABLE
1263:      CALL DCS(M,F,X)
1264:      RETURN
1265:      ENDIF
1266: C -----
1267:      IF (KF.EQ.19) THEN
1268: C      FACTORIAL FUNCTION, MIN = 0 AT X=(1,2,3,...,M)
1269:      CALL FACTOR1(M,F,X)
1270:      RETURN
1271:      ENDIF
1272: C -----
1273:      IF (KF.EQ.20) THEN

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1274: C      DECANOMIAL FUNCTION, MIN =0 AT X=(2, -3)
1275:         DO I=1,M
1276:         IF (DABS(X(I)) .GT. 4.D00) THEN
1277:         CALL RANDOM(RAND)
1278:         X(I)= (RAND-0.5D00)*8
1279:         ENDDIF
1280:         ENDDO
1281:         CALL DECANOM(M,F,X)
1282:         RETURN
1283:         ENDDIF
1284: C      -----
1285:         IF (KF.EQ.21) THEN
1286: C      JUDGE'S FUNCTION F(0.864, 1.23) = 16.0817; M=2
1287:         CALL JUDGE(M,X,F)
1288:         RETURN
1289:         ENDDIF
1290: C      -----
1291:         IF (KF.EQ.22) THEN
1292: C      DODECAL FUNCTION
1293:         CALL DODECAL(M,F,X)
1294:         RETURN
1295:         ENDDIF
1296: C      -----
1297:         IF (KF.EQ.23) THEN
1298: C      WHEN X(1)*X(2)=X(1)*X(2) ? M=2
1299:         CALL SEQP(M,F,X)
1300:         RETURN
1301:         ENDDIF
1302: C      -----
1303:         IF (KF.EQ.24) THEN
1304: C      WHEN ARITHMETIC MEAN = GEOMETRIC MEAN ? : M =>1
1305:         CALL AMGM(M,F,X)
1306:         RETURN
1307:         ENDDIF
1308: C      -----
1309:         IF (KF.EQ.25) THEN
1310: C      M =>2
1311:         CALL FUNCT2(M,F,X)
1312:         RETURN
1313:         ENDDIF
1314: C      -----
1315:         IF (KF.EQ.26) THEN
1316: C      M =>2
1317:         CALL FUNCT3(M,F,X)
1318:         RETURN
1319:         ENDDIF
1320: C      -----
1321:         IF (KF.EQ.27) THEN
1322: C      M =>2
1323:         CALL FUNCT4(M,F,X)
1324:         RETURN
1325:         ENDDIF
1326: C      -----
1327:         IF (KF.EQ.28) THEN
1328: C      M =>2
1329:         CALL FUNCT6(M,F,X)
1330:         RETURN
1331:         ENDDIF
1332: C      -----
1333:         IF (KF.EQ.29) THEN
1334: C      M =>2
1335:         CALL FUNCT7(M,F,X)
1336:         RETURN
1337:         ENDDIF
1338: C      -----
1339:         IF (KF.EQ.30) THEN
1340: C      M =>2

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1341:      CALL FUNCT12 (M, F, X)
1342:      RETURN
1343:      ENDIF
1344: C -----
1345:      IF (KF.EQ.31) THEN
1346: C      M =>2
1347:      CALL FUNCT13 (M, F, X)
1348:      RETURN
1349:      ENDIF
1350: C -----
1351:      IF (KF.EQ.32) THEN
1352: C      M =2
1353:      CALL FUNCT14 (M, F, X)
1354:      RETURN
1355:      ENDIF
1356: C -----
1357:      IF (KF.EQ.33) THEN
1358: C      M =4
1359:      CALL FUNCT15 (M, F, X)
1360:      RETURN
1361:      ENDIF
1362: C -----
1363:      IF (KF.EQ.34) THEN
1364: C      WOOD FUNCTION : F MIN : M=4
1365:      CALL WOOD (M, X, F)
1366:      RETURN
1367:      ENDIF
1368: C -----
1369:      IF (KF.EQ.35) THEN
1370: C      FENTON & EASON FUNCTION : : M=2
1371:      CALL FENTONEASON (M, X, F)
1372:      RETURN
1373:      ENDIF
1374: C -----
1375:      IF (KF.EQ.36) THEN
1376: C      HOUGEN FUNCTION 5 VARIABLES : M =3
1377:      CALL HOUGEN (X, M, F)
1378:      RETURN
1379:      ENDIF
1380: C -----
1381:      IF (KF.EQ.37) THEN
1382: C      GIUNTA FUNCTION 2 VARIABLES :M =2
1383:      CALL GIUNTA (M, X, F)
1384:      RETURN
1385:      ENDIF
1386: C -----
1387:      IF (KF.EQ.38) THEN
1388: C      EGGHOLDER FUNCTION M VARIABLES
1389:      CALL EGGHOLD (M, X, F)
1390:      RETURN
1391:      ENDIF
1392: C -----
1393:      IF (KF.EQ.39) THEN
1394: C      TRID FUNCTION M VARIABLES
1395:      CALL TRID (M, X, F)
1396:      RETURN
1397:      ENDIF
1398: C -----
1399:      IF (KF.EQ.40) THEN
1400: C      GRIEWANK FUNCTION M VARIABLES
1401:      CALL GRIEWANK (M, X, F)
1402:      RETURN
1403:      ENDIF
1404: C -----
1405:      IF (KF.EQ.41) THEN
1406: C      WEIERSTRASS FUNCTION M VARIABLES
1407:      CALL WEIERSTRASS (M, X, F)

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1408:      RETURN
1409:      ENDIF
1410: C -----
1411:      IF (KF.EQ.42) THEN
1412: C      LEVY-3 FUNCTION 2 VARIABLES
1413:      CALL LEVY3 (M, X, F)
1414:      RETURN
1415:      ENDIF
1416: C -----
1417:      IF (KF.EQ.43) THEN
1418: C      LEVY-5 FUNCTION 2 VARIABLES
1419:      CALL LEVY5 (M, X, F)
1420:      RETURN
1421:      ENDIF
1422: C -----
1423:      IF (KF.EQ.44) THEN
1424: C      LEVY-8 FUNCTION 3 VARIABLES
1425:      CALL LEVY8 (M, X, F)
1426:      RETURN
1427:      ENDIF
1428: C -----
1429:      IF (KF.EQ.45) THEN
1430: C      RASTRIGIN FUNCTION M VARIABLES
1431:      CALL RASTRIGIN (M, X, F)
1432:      RETURN
1433:      ENDIF
1434: C -----
1435:      IF (KF.EQ.46) THEN
1436: C      ACKLEY FUNCTION M VARIABLES
1437:      CALL ACKLEY (M, X, F)
1438:      RETURN
1439:      ENDIF
1440: C -----
1441:      IF (KF.EQ.47) THEN
1442: C      MICHALEWICZ FUNCTION M VARIABLES
1443:      CALL MICHALEWICZ (M, X, F)
1444:      RETURN
1445:      ENDIF
1446: C -----
1447:      IF (KF.EQ.48) THEN
1448: C      SCHWEFEL FUNCTION M VARIABLES
1449:      CALL SCHWEFEL (M, X, F)
1450:      RETURN
1451:      ENDIF
1452: C -----
1453:      IF (KF.EQ.49) THEN
1454: C      SHUBERT FUNCTION 2 VARIABLES
1455:      CALL SHUBERT (M, X, F)
1456:      RETURN
1457:      ENDIF
1458: C -----
1459:      IF (KF.EQ.50) THEN
1460: C      DIXON AND PRICE FUNCTION M VARIABLES
1461:      CALL DIXPRICE (M, X, F)
1462:      RETURN
1463:      ENDIF
1464: C -----
1465:      IF (KF.EQ.51) THEN
1466: C      SHEKEL FUNCTION 4 VARIABLES
1467:      CALL SHEKEL (M, X, F)
1468:      RETURN
1469:      ENDIF
1470: C -----
1471:      IF (KF.EQ.52) THEN
1472: C      PAVIANI FUNCTION 10 VARIABLES
1473:      CALL PAVIANI (M, X, F)
1474:      RETURN
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1475:      ENDIF
1476: C -----
1477:      IF (KF.EQ.53) THEN
1478: C      BRANIN FUNCTION#1 2 VARIABLES
1479:      CALL BRANIN1 (M, X, F)
1480:      RETURN
1481:      ENDIF
1482: C -----
1483:      IF (KF.EQ.54) THEN
1484: C      BRANIN FUNCTION#2 2 VARIABLES
1485:      CALL BRANIN2 (M, X, F)
1486:      RETURN
1487:      ENDIF
1488: C -----
1489:      IF (KF.EQ.55) THEN
1490: C      BOHACHEVSKY FUNCTION#1 2 VARIABLES
1491:      CALL BOHACHEVSKY1 (M, X, F)
1492:      RETURN
1493:      ENDIF
1494: C -----
1495:      IF (KF.EQ.56) THEN
1496: C      BOHACHEVSKY FUNCTION#2 2 VARIABLES
1497:      CALL BOHACHEVSKY2 (M, X, F)
1498:      RETURN
1499:      ENDIF
1500: C -----
1501:      IF (KF.EQ.57) THEN
1502: C      BOHACHEVSKY FUNCTION#3 2 VARIABLES
1503:      CALL BOHACHEVSKY3 (M, X, F)
1504:      RETURN
1505:      ENDIF
1506: C -----
1507:      IF (KF.EQ.58) THEN
1508: C      EASOM FUNCTION#3 2 VARIABLES
1509:      CALL EASOM (M, X, F)
1510:      RETURN
1511:      ENDIF
1512: C -----
1513:      IF (KF.EQ.59) THEN
1514: C      ROSENBROCK FUNCTION M VARIABLES
1515:      CALL ROSENBROCK (M, X, F)
1516:      RETURN
1517:      ENDIF
1518: C -----
1519:      IF (KF.EQ.60) THEN
1520: C      CROSS-LEGGED TABLE FUNCTION : 2 VARIABLES
1521:      CALL CROSSLEG (M, X, F)
1522:      RETURN
1523:      ENDIF
1524: C -----
1525:      IF (KF.EQ.61) THEN
1526: C      CROSS FUNCTION : 2 VARIABLES
1527:      CALL CROSS (M, X, F)
1528:      RETURN
1529:      ENDIF
1530: C -----
1531:      IF (KF.EQ.62) THEN
1532: C      CROSS-IN-TRAY FUNCTION : 2 VARIABLES
1533:      CALL CROSSINTRAY (M, X, F)
1534:      RETURN
1535:      ENDIF
1536: C -----
1537:      IF (KF.EQ.63) THEN
1538: C      CROWNED-CROSS FUNCTION : 2 VARIABLES
1539:      CALL CROWNEDCROSS (M, X, F)
1540:      RETURN
1541:      ENDIF
```

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1542: C -----
1543: C IF (KF.EQ.64) THEN
1544: C TT-HOLDER FUNCTION : 2 VARIABLES, MIN F ([+/-]1.5706, 0) = -10.8723
1545: C CALL TTHOLDER (M, X, F)
1546: C RETURN
1547: C ENDIF
1548: C -----
1549: C IF (KF.EQ.65) THEN
1550: C HOLDER-TABLE FUNCTION : 2 VARIABLES
1551: C MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -26.92034 APPROX
1552: C CALL HOLDERTABLE (M, X, F)
1553: C RETURN
1554: C ENDIF
1555: C -----
1556: C IF (KF.EQ.66) THEN
1557: C CARROM-TABLE FUNCTION : 2 VARIABLES
1558: C MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -24.15682 APPROX
1559: C CALL CARROMTABLE (M, X, F)
1560: C RETURN
1561: C ENDIF
1562: C -----
1563: C IF (KF.EQ.67) THEN
1564: C PEN-HOLDER FUNCTION : 2 VARIABLES
1565: C MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -0.963535 APPROX
1566: C CALL PENHOLDER (M, X, F)
1567: C RETURN
1568: C ENDIF
1569: C -----
1570: C IF (KF.EQ.68) THEN
1571: C BIRD FUNCTION : 2 VARIABLES
1572: C MIN F (4.70104, 3.15294) APPROX = -106.764537 APPROX OR
1573: C MIN F (-1.58214, -3.13024) APPROX = -106.764537 APPROX
1574: C CALL BIRD (M, X, F)
1575: C RETURN
1576: C ENDIF
1577: C -----
1578: C IF (KF.EQ.69) THEN
1579: C CHICHINADZE FUNCTION : -30 <=X(I)<= 30; M=2
1580: C MIN F (5.901329, 0.5) = -43.3158621
1581: C CALL CHICHINADZE (M, X, F)
1582: C RETURN
1583: C ENDIF
1584: C -----
1585: C IF (KF.EQ.70) THEN
1586: C MCCORMICK FUNCTION : -1.5<= X(1)<=4; -3<=X(2)<=4 ; M=2
1587: C MIN F (-0.54719755, -1.54719755) = -1.913223 APPROX
1588: C CALL MCCORMICK (M, X, F)
1589: C RETURN
1590: C ENDIF
1591: C -----
1592: C IF (KF.EQ.71) THEN
1593: C GLANKWAHMDEE FUNCTION:
1594: C CALL GLANKWAHMDEE (M, X, F)
1595: C RETURN
1596: C ENDIF
1597: C -----
1598: C IF (KF.EQ.72) THEN
1599: C FLETCHER-POWELL FUNCTION
1600: C CALL FLETCHER (M, X, F)
1601: C RETURN
1602: C ENDIF
1603: C -----
1604: C IF (KF.EQ.73) THEN
1605: C POWELL FUNCTION
1606: C CALL POWELL (M, X, F)
1607: C RETURN
1608: C ENDIF

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1609: C -----
1610: IF (KF.EQ.74) THEN
1611: C HARTMANN FUNCTION
1612: CALL HARTMANN (M, X, F)
1613: RETURN
1614: ENDIF
1615: C -----
1616: IF (KF.EQ.75) THEN
1617: C COVILLE FUNCTION
1618: CALL COLVILLE (M, X, F)
1619: RETURN
1620: ENDIF
1621: C -----
1622: IF (KF.EQ.76) THEN
1623: C HIMMELBLAU FUNCTION
1624: CALL HIMMELBLAU (M, X, F)
1625: RETURN
1626: ENDIF
1627: C -----
1628: IF (KF.EQ.77) THEN
1629: C BEALE FUNCTION
1630: CALL BEALE (M, X, F)
1631: RETURN
1632: ENDIF
1633: C -----
1634: IF (KF.EQ.78) THEN
1635: C BOOTH FUNCTION
1636: CALL BOOTH (M, X, F)
1637: RETURN
1638: ENDIF
1639: C -----
1640: IF (KF.EQ.79) THEN
1641: C HUMP FUNCTION
1642: CALL HUMP (M, X, F)
1643: RETURN
1644: ENDIF
1645: C -----
1646: IF (KF.EQ.80) THEN
1647: C MATYAS FUNCTION
1648: CALL MATYAS (M, X, F)
1649: RETURN
1650: ENDIF
1651: C -----
1652: IF (KF.EQ.81) THEN
1653: C MISHRA_1 FUNCTION
1654: CALL MISHRA_1 (M, X, F)
1655: RETURN
1656: ENDIF
1657: C -----
1658: IF (KF.EQ.82) THEN
1659: C MISHRA_2 FUNCTION
1660: CALL MISHRA_2 (M, X, F)
1661: RETURN
1662: ENDIF
1663: C -----
1664: IF (KF.EQ.83) THEN
1665: C ZAKHAROV FUNCTION
1666: CALL ZAKHAROV (M, X, F)
1667: RETURN
1668: ENDIF
1669: C -----
1670: IF (KF.EQ.84) THEN
1671: C MULTOMOD FUNCTION
1672: CALL MULTIMOD (M, X, F)
1673: RETURN
1674: ENDIF
1675: C -----
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1743: C      FIND X(I), I=1,2,...,M SUCH THAT THEIR PRODUCT IS EQUAL TO FACT.
1744: C      LARGER THE VALUE OF M (=>8) OR SO, HARDER IS THE PROBLEM
1745:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1746:      DIMENSION X(*)
1747:      F=0.D00
1748:      FACT=1.D00
1749:      P=1.D00
1750:      DO I=1,M
1751:      FACT=FACT*I
1752:      P=P*X(I)
1753:      F=F+DABS(P-FACT)**2
1754:      ENDDO
1755:      RETURN
1756:      END
1757: C      -----
1758:      SUBROUTINE DECANOM(M,F,X)
1759: C      DECANOMIAL FUNCTION; MIN (2, -3) = 0
1760:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1761:      DIMENSION X(*)
1762:      F1= DABS(X(1)**10-20*X(1)**9+180*X(1)**8-960*X(1)**7+
1763: & 3360*X(1)**6-8064*X(1)**5+13340*X(1)**4-15360*X(1)**3+
1764: & 11520*X(1)**2-5120*X(1)+2624.D00)
1765:      F2= DABS(X(2)**4+12*X(2)**3+54*X(2)**2+108*X(2)+81.D00)
1766:      F=0.001D00*(F1+F2)**2
1767:      RETURN
1768:      END
1769: C      -----
1770:      SUBROUTINE JUDGE(M,X,F)
1771:      PARAMETER (N=20)
1772: C      THIS SUBROUTINE IS FROM THE EXAMPLE IN JUDGE ET AL., THE THEORY
1773: C      AND PRACTICE OF ECONOMETRICS, 2ND ED., PP. 956-7. THERE ARE TWO
1774: C      OPTIMA: F(0.86479,1.2357)=16.0817307 (WHICH IS THE GLOBAL MINIMUM)
1775: C      AND F(2.35,-0.319)=20.9805 (WHICH IS LOCAL). ADAPTED FROM BILL
1776: C      GOFFE'S SIMMAN (SIMULATED ANNEALING) PROGRAM
1777:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1778:      DIMENSION Y(N), X2(N), X3(N), X(*)
1779:      DATA (Y(I),I=1,N)/4.284,4.149,3.877,0.533,2.211,2.389,2.145,
1780: & 3.231,1.998,1.379,2.106,1.428,1.011,2.179,2.858,1.388,1.651,
1781: & 1.593,1.046,2.152/
1782:      DATA (X2(I),I=1,N)/.286,.973,.384,.276,.973,.543,.957,.948,.543,
1783: & .797,.936,.889,.006,.828,.399,.617,.939,.784,.072,.889/
1784:      DATA (X3(I),I=1,N)/.645,.585,.310,.058,.455,.779,.259,.202,.028,
1785: & .099,.142,.296,.175,.180,.842,.039,.103,.620,.158,.704/
1786:
1787:      F=0.D00
1788:      DO I=1,N
1789:      F=F+(X(1) + X(2)*X2(I) + (X(2)**2)*X3(I) - Y(I))**2
1790:      ENDDO
1791:      RETURN
1792:      END
1793: C      -----
1794:      SUBROUTINE DODECAL(M,F,X)
1795:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1796:      DIMENSION X(*)
1797: C      DODECAL POLYNOMIAL MIN F(1,2,3)=0
1798:      DO I=1,M
1799:      IF (DABS(X(I)) .GT. 5.D0) THEN
1800:      CALL RANDOM(RAND)
1801:      X(I)=(RAND-0.5D00)*10
1802:      ENDIF
1803:      ENDDO
1804:      F=0.D00
1805:      F1=2*X(1)**3+5*X(1)*X(2)+4*X(3)-2*X(1)**2*X(3)-18.D00
1806:      F2=X(1)+X(2)**3+X(1)*X(2)**2+X(1)*X(3)**2-22.D00
1807:      F3=8*X(1)**2+2*X(2)*X(3)+2*X(2)**2+3*X(2)**3-52.D00
1808:      F=(F1*F3*F2**2+F1*F2*F3**2+F2**2+(X(1)+X(2)-X(3))**2)**2
1809:      RETURN

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1810:      END
1811: C      -----
1812:      SUBROUTINE SEQP(M,F,X)
1813:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1814:      DIMENSION X(*)
1815: C      FOR WHAT VALUES  $X(1)+X(2)=X(1)*X(2)$  ? ANSWER: FOR (0,0) AND (2,2)
1816: C      WHILE X(1), X(2) ARE INTEGERS.
1817:      X(1)=INT(X(1)) ! X(1) CONVERTED TO INTEGER
1818:      X(2)=INT(X(2)) ! X(2) CONVERTED TO INTEGER
1819:
1820:      F1=X(1)+X(2)
1821:      F2=X(1)*X(2)
1822:      F=(F1-F2)**2 ! TURN ALIVE THIS XOR
1823: C      F=DABS(F1-F2) ! TURN ALIVE THIS - BUT NOT BOTH -----
1824:      RETURN
1825:      END
1826: C      -----
1827:      SUBROUTINE AMGM(M,F,X)
1828:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1829:      DIMENSION X(*)
1830: C      FOR WHAT VALUES ARITHMETIC MEAN = GEOMETRIC MEAN ? THE ANSWER IS:
1831: C      IF  $X(1)=X(2)=\dots=X(M)$  AND ALL X ARE NON-NEGATIVE
1832: C      TAKE ONLY THE ABSOLUTE VALUES OF X
1833:      SUM=0.D00
1834:      DO I=1,M
1835:      X(I)=DABS(X(I))
1836:      ENDDO
1837: C      SET SUM = SOME POSITIVE NUMBER. THIS MAKES THE FUNCTION UNIMODAL
1838:      SUM= 100.D00 ! TURNED ALIVE FOR UNIQUE MINIMUM AND SET SUM TO
1839: C      SOME POSITIVE NUMBER. HERE IT IS 100; IT COULD BE ANYTHING ELSE.
1840:      F1=0.D00
1841:      F2=1.D00
1842:      DO I=1,M
1843:      F1=F1+X(I)
1844:      F2=F2*X(I)
1845:      ENDDO
1846:      XSUM=F1
1847:      F1=F1/M ! SUM DIVIDED BY M = ARITHMETIC MEAN
1848:      F2=F2**(1.D00/M) ! MTH ROOT OF THE PRODUCT = GEOMETRIC MEAN
1849:      F=(F1-F2)**2
1850:      IF (SUM.GT.0.D00) F=F+(SUM-XSUM)**2
1851:      RETURN
1852:      END
1853: C      -----
1854:      SUBROUTINE FUNCT2(M,F,X)
1855: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1856: C      IN FOGEL, L.J., ANGELIN, P.J. AND BACK, T. (ED) PROCEEDINGS OF THE
1857: C      FIFTH ANNUAL CONFERENCE ON EVOLUTIONARY PROGRAMMING, PP. 451-460,
1858: C      MIT PRESS, CAMBRIDGE, MASS.
1859: C       $\min F(0, 0, \dots, 0) = 0$ 
1860:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1861:      DIMENSION X(*)
1862:      F=0.D00
1863:      F1=1.D00
1864:      DO I=1,M
1865:      IF (DABS(X(I)).GT.10.D00) THEN
1866:      CALL RANDOM(RAND)
1867:      X(I)=(RAND-.5D00)*20
1868:      ENDIF
1869:      ENDDO
1870:      DO I=1,M
1871:      F=F+DABS(X(I))
1872:      F1=F1*DABS(X(I))
1873:      ENDDO
1874:      F=F+F1
1875:      RETURN
1876:      END

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1877: C -----
1878: SUBROUTINE FUNCT3(M,F,X)
1879: C REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1880: C MIN F(0, 0, ..., 0) = 0
1881: IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1882: DIMENSION X(*)
1883: F=0.D00
1884: F1=0.D00
1885: DO I=1,M
1886: IF(DABS(X(I)).GT.100.D00) THEN
1887: CALL RANDOM(RAND)
1888: X(I)=(RAND-.5D00)*200
1889: ENDF
1890: ENDDO
1891: DO I=1,M
1892: F1=0.D00
1893: DO J=1,I
1894: F1=F1+X(J)**2
1895: ENDDO
1896: F=F+F1
1897: ENDDO
1898: RETURN
1899: END
1900: C -----
1901: SUBROUTINE FUNCT4(M,F,X)
1902: C REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1903: C MIN F(0, 0, ..., 0) = 0
1904: IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1905: DIMENSION X(*)
1906: F=0.D00
1907: DO I=1,M
1908: IF(X(I).LT.0.D00 .OR. X(I).GE.M) THEN
1909: CALL RANDOM(RAND)
1910: X(I)=RAND*2*M
1911: ENDF
1912: ENDDO
1913: C FIND MAX(X(I))=MAX(ABS(X(I))) NOTE: HERE X(I) CAN BE ONLY POSITIVE
1914: XMAX=X(1)
1915: DO I=1,M
1916: IF(XMAX.LT.X(I)) XMAX=X(I)
1917: ENDDO
1918: F=XMAX
1919: RETURN
1920: END
1921: C -----
1922: SUBROUTINE FUNCT6(M,F,X)
1923: C REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1924: C MIN F(-.5, -.5, ..., -.5) = 0
1925: IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1926: DIMENSION X(*)
1927: F=0.D00
1928: DO I=1,M
1929: IF(DABS(X(I)).GT.100.D00) THEN
1930: CALL RANDOM(RAND)
1931: X(I)=(RAND-.5D00)*200
1932: ENDF
1933: ENDDO
1934: DO I=1,M
1935: F=F+(X(I)+0.5D00)**2
1936: ENDDO
1937: RETURN
1938: END
1939: C -----
1940: SUBROUTINE FUNCT7(M,F,X)
1941: C REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1942: C MIN F(0, 0, ..., 0) = 0
1943: IMPLICIT DOUBLE PRECISION (A-H, O-Z)

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1944:      COMMON /RNDM/IU,IV
1945:      INTEGER IU,IV
1946:      DIMENSION X(*)
1947:      F=0.D00
1948:      DO I=1,M
1949:          IF (DABS(X(I)).GT.1.28D00) THEN
1950:              CALL RANDOM(RAND)
1951:              X(I)=(RAND-0.5D00)*2.56D00
1952:          ENDIF
1953:      ENDDO
1954:      DO I=1,M
1955:          CALL RANDOM(RAND)
1956:          F=F+(I*X(I)**4)
1957:      ENDDO
1958:          CALL RANDOM(RAND)
1959:          F=F+RAND
1960:      RETURN
1961:      END
1962: C -----
1963:      SUBROUTINE FUNCT12(M,F,X)
1964: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
1965:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
1966:      DIMENSION X(100),Y(100)
1967:      DATA A,B,C /10.D00,100.D00,4.D00/
1968:      PI=4.D00*DATAN(1.D00)
1969:      F=0.D00
1970: C      MIN F (-1, -1, -1, ..., -1) = 0
1971: C      X(I)=-1.D00 ! TO CHECK, TURN IT ALIVE
1972:      DO I=1,M
1973:          IF (DABS(X(I)).GT.50.D00) THEN
1974:              CALL RANDOM(RAND)
1975:              X(I)=(RAND-0.5D00)*100.D00
1976:          ENDIF
1977:      ENDDO
1978:      F1=0.D00
1979:      DO I=1,M
1980:          XX=DABS(X(I))
1981:          U=0.D00
1982:          IF (XX.GT.A) U=B*(XX-A)**4
1983:          F1=F1+U
1984:      ENDDO
1985:      F2=0.D00
1986:      DO I=1,M-1
1987:          Y(I)=1.D00+.25D00*(X(I)+1.D00)
1988:          F2=F2+(Y(I)-1.D00)**2*(1.D00+10.D00*(DSIN(PI*X(I+1)))**2)
1989:      ENDDO
1990:          Y(M)=1.D00+.25D00*(X(M)+1.D00)
1991:          F3=(Y(M)-1.D00)**2
1992:          Y(1)=1.D00+.25D00*(X(1)+1.D00)
1993:          F4=10.D00*(DSIN(PI*Y(1)))**2
1994:          F=(PI/M)*(F4+F2+F3)+F1
1995:      RETURN
1996:      END
1997: C -----
1998:      SUBROUTINE FUNCT13(M,F,X)
1999: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
2000:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2001:      DIMENSION X(100)
2002:      DATA A,B,C /5.D00,100.D00,4.D00/
2003:      PI=4*DATAN(1.D00)
2004:      F=0.D00
2005: C      MIN F (1, 1, 1, ..., 4.7544 APPROX) = -1.15044 APPROX
2006: C      X(I)=1.D00 ! TO CHECK, TURN IT ALIVE
2007: C      X(M)=-4.7544 ! TO CHECK, TURN IT ALIVE
2008:      DO I=1,M
2009:          IF (DABS(X(I)).GT.50.D00) THEN
2010:              CALL RANDOM(RAND)

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2011:      X(I)=(RAND-.5D00)*100.D00
2012:      ENDF
2013:      ENDDO
2014:      F1=0.D00
2015:      DO I=1,M
2016:      XX=DABS(X(I))
2017:      U=0.D00
2018:      IF(XX.GT.A) U=B*(XX-A)**C
2019:      F1=F1+U
2020:      ENDDO
2021:      F2=0.D00
2022:      DO I=1,M-1
2023:      F2=F2+(X(I)-1.D00)**2*(1.D00+(DSIN(3*PI*X(I+1)))**2))
2024:      ENDDO
2025:      F3=(X(M)-1.D00)*(1.D00+(DSIN(2*PI*X(M)))**2)
2026:      F4=(DSIN(3*PI*X(1)))**2
2027:      F=0.1*(F4+F2+F3)+F1
2028:      RETURN
2029:      END
2030: C -----
2031:      SUBROUTINE FUNCT14(M,F,X)
2032: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
2033: C      MIN F (-31.98, 31.98) = 0.998
2034:      PARAMETER (N=25,NN=2)
2035:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2036:      DIMENSION X(2), A(NN,N)
2037:      DATA (A(1,J),J=1,N) /-32.D00,-16.D00,0.D00,16.D00,32.D00,-32.D00,
& -16.D00,0.D00,16.D00,32.D00,-32.D00,-16.D00,0.D00,16.D00,32.D00,
2039: & -32.D0,-16.D0,0.D0,16.D0,32.D0,-32.D0,-16.D0,0.D0,16.D0,32.D0/
2040:      DATA (A(2,J),J=1,N) /-32.D00,-32.D00,-32.D00,-32.D00,-32.D00,
& -16.D00,-16.D00,-16.D00,-16.D00,-16.D00,0.D00,0.D00,0.D00,0.D00,
2042: & 0.D00,16.D00,16.D00,16.D00,16.D00,16.D00,32.D00,32.D00,
& 32.D00,32.D00,32.D00/
2044:
2045:      F=0.D00
2046:      DO I=1,M
2047:      IF(DABS(X(I)).GT.100.D00) THEN
2048:      CALL RANDOM(RAND)
2049:      X(I)=(RAND-.5D00)*200.D00
2050:      ENDF
2051:      ENDDO
2052:      F1=0.D00
2053:      DO J=1,N
2054:      F2=0.D00
2055:      DO I=1,2
2056:      F2=F2+(X(I)-A(I,J))**6
2057:      ENDDO
2058:      F2=1.D00/(J+F2)
2059:      F1=F1+F2
2060:      ENDDO
2061:      F=1.D00/(0.002D00+F1)
2062:      RETURN
2063:      END
2064: C -----
2065:      SUBROUTINE FUNCT15(M,F,X)
2066: C      REF: YAO, X. AND LIU, Y. (1996): FAST EVOLUTIONARY PROGRAMMING
2067: C      MIN F(.19, .19, .12, .14) = 0.3075
2068:      PARAMETER (N=11)
2069:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2070:      DIMENSION X(*), A(N),B(N)
2071:      DATA (A(I),I=1,N) /.1957D00,.1947D00,.1735D00,.16D00,.0844D00,
& .0627D00,.0456D00,.0342D00,.0323D00,.0235D00,.0246D00/
2073:      DATA (B(I),I=1,N) /0.25D00,0.5D00,1.D00,2.D00,4.D00,6.D00,8.D00,
& 10.D00,12.D00,14.D00,16.D00/
2075:      DO I=1,N
2076:      B(I)=1.D00/B(I)
2077:      ENDDO

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2078:      F=0.D00
2079:      DO I=1,M
2080:      IF (DABS(X(I)).GT.5.D00) THEN
2081:      CALL RANDOM(RAND)
2082:      X(I)=(RAND-.5D00)*10.D00
2083:      ENDIF
2084:      ENDDO
2085:      DO I=1,N
2086:      F1=X(1)*(B(I)**2+B(I)*X(2))
2087:      F2=B(I)**2+B(I)*X(3)+X(4)
2088:      F=F+(A(I)-F1/F2)**2
2089:      ENDDO
2090:      F=F*1000
2091:      RETURN
2092:      END
2093: C -----
2094:      SUBROUTINE LINPROG1(M,F,X)
2095: C      LINEAR PROGRAMMING : MINIMIZATION PROBLEM
2096: C      IN THIS PROBLEM : M = NO. OF DECISION VARIABLES = 2
2097: C      MIN F (2.390, 2.033) = -19.7253 APPROX
2098: C      MIN F = OVER J=1, M : DO SUM(A(I,J)*X(J)) SUBJECT TO CONSTRAINTS
2099: C      OVER J=1, M : DO SUM(A(I,J)*X(J)) <= C(I) ; I=2
2100: C      . . . . .
2101: C      OVER J=1, M : DO SUM(A(I,J)*X(J)) <= C(I) ; I=N
2102: C      ALL X(I) => 0
2103:      PARAMETER (N=3) ! N IS THE NO. OF CONSTRAINTS + 1
2104:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2105:      DIMENSION X(*),A(20,10),C(20),FF(20)
2106:      DATA (A(1,J),J=1,2),C(1)/4.D0,5.D0,0.0D0/!COEFF OF OBJ FUNCTION
2107:      DATA (A(2,J),J=1,2),C(2)/10.D0,3.D0,30D0/!COEFF OF 1ST CONSTRAINT
2108:      DATA (A(3,J),J=1,2),C(3)/6.D0,20.D0,55.D0/!COEFF OF 2ND CONSTRAINT
2109: C -----
2110: C      USING ONLY NON-NEGATIVE VALUES OF X(I)
2111:      DO I=1,M
2112:      X(I)=DABS(X(I))
2113:      ENDDO
2114: C      EVALUATION OF OBJ FUNCTION AND CONSTRAINTS
2115:      DO I=1,N
2116:      FF(I)=0.D00
2117:      DO J=1,M
2118:      FF(I)=FF(I)+A(I,J)*X(J)
2119:      ENDDO
2120:      ENDDO
2121:      F=-FF(1) ! CHANGE OF SIGN FOR MINIMIZATION
2122: C      CHECK FOR SATISFYING OR VIOLATING THE CONSTRAINTS
2123:      DO I=2,N
2124:      FF(I)=FF(I)-C(I) ! SLACK
2125: C      PENALTY FOR CROSSING LIMITS
2126:      IF (FF(I).GT.0) F=F+(10+FF(I))**2
2127:      ENDDO
2128:      RETURN
2129:      END
2130: C -----
2131:      SUBROUTINE LINPROG2(M,F,X)
2132: C      LINEAR PROGRAMMING : MINIMIZATION PROBLEM
2133: C      IN THIS PROBLEM : M = NO. OF DECISION VARIABLES = 3
2134: C      MIN F (250, 625, 0) = -3250
2135: C      MIN F = OVER J=1, M : DO SUM(A(I,J)*X(J)) SUBJECT TO CONSTRAINTS
2136: C      OVER J=1, M : DO SUM(A(I,J)*X(J)) <= C(I) ; I=2
2137: C      . . . . .
2138: C      OVER J=1, M : DO SUM(A(I,J)*X(J)) <= C(I) ; I=N
2139: C      ALL X(I) => 0
2140:      PARAMETER (N=4) ! N IS THE NO. OF CONSTRAINTS + 1
2141:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2142:      DIMENSION X(*),A(20,10),C(20),FF(20)
2143:      DATA (A(1,J),J=1,3),C(1)/30.D0,40.D0,20.D0,0.0D0/! COEFF OF OBJ FUNCTION
2144:      DATA (A(2,J),J=1,3),C(2)/10.D0,12.D0,7.D0,10000.0D0/!COEFF OF 1ST CONSTRAINT

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2145: DATA (A(3,J),J=1,3),C(3)/7.D0,10.D0,8.D0,8000.D0/! COEFF OF 2ND CONSTRAINT
2146: DATA (A(4,J),J=1,3),C(4)/1.D0,1.D0,1.D0,1000.D0/! COEFF OF 3RD CONSTRAINT
2147: C -----
2148: C USING ONLY NON-NEGATIVE VALUES OF X(I)
2149: DO I=1,M
2150: X(I)=DABS(X(I))
2151: ENDDO
2152: C EVALUATION OF OBJ FUNCTION AND CONSTRAINTS
2153: DO I=1,N
2154: FF(I)=0.D00
2155: DO J=1,M
2156: FF(I)=FF(I)+A(I,J)*X(J)
2157: ENDDO
2158: ENDDO
2159: F=-FF(1) ! CHANGE OF SIGN FOR MINIMIZATION
2160: C CHECK FOR SATISFYING OR VIOLATING THE CONSTRAINTS
2161: DO I=2,N
2162: FF(I)=FF(I)-C(I) ! SLACK
2163: C PENALTY FOR CROSSING LIMITS
2164: IF (FF(I) .GT. 0.D00) F=F+(100.D00+FF(I))**2
2165: ENDDO
2166: RETURN
2167: END
2168: C -----
2169: SUBROUTINE HOUGEN(A,M,F)
2170: PARAMETER(N=13,K=3)
2171: IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2172: DIMENSION X(N,K),RATE(N),A(*)
2173: C -----
2174: C HOUGEN FUNCTION (HOUGEN-WATSON MODEL FOR REACTION KINATICS)
2175: C NO. OF PARAMETERS (A) TO ESTIMATE = 5 = M
2176:
2177: C BEST RESULTS ARE:
2178: C A(1)=1.253031; A(2)=1.190943; A(3)=0.062798; A(4)=0.040063
2179: C A(5)=0.112453 ARE BEST ESTIMATES OBTAINED BY ROSENBROCK &
2180: C QUASI-NEWTON METHOD WITH SUM OF SQUARES OF DEVIATION =0.298900994
2181: C AND R=0.99945.
2182:
2183: C THE NEXT BEST RESULTS GIVEN BY HOOKE-JEEVES & QUASI-NEWTON
2184: C A(1)=2.475221;A(2)=0.599177; A(3)=0.124172; A(4)=0.083517
2185: C A(5)=0.217886; SUM OF SQUARES OF DEVIATION = 0.318593458
2186: C R=0.99941
2187: C MOST OF THE OTHER METHODS DO NOT PERFORM WELL
2188: C -----
2189: DATA X(1,1),X(1,2),X(1,3),RATE(1) /470,300,10,8.55/
2190: DATA X(2,1),X(2,2),X(2,3),RATE(2) /285,80,10,3.79/
2191: DATA X(3,1),X(3,2),X(3,3),RATE(3) /470,300,120,4.82/
2192: DATA X(4,1),X(4,2),X(4,3),RATE(4) /470,80,120,0.02/
2193: DATA X(5,1),X(5,2),X(5,3),RATE(5) /470,80,10,2.75/
2194: DATA X(6,1),X(6,2),X(6,3),RATE(6) /100,190,10,14.39/
2195: DATA X(7,1),X(7,2),X(7,3),RATE(7) /100,80,65,2.54/
2196: DATA X(8,1),X(8,2),X(8,3),RATE(8) /470,190,65,4.35/
2197: DATA X(9,1),X(9,2),X(9,3),RATE(9) /100,300,54,13/
2198: DATA X(10,1),X(10,2),X(10,3),RATE(10) /100,300,120,8.5/
2199: DATA X(11,1),X(11,2),X(11,3),RATE(11) /100,80,120,0.05/
2200: DATA X(12,1),X(12,2),X(12,3),RATE(12) /285,300,10,11.32/
2201: DATA X(13,1),X(13,2),X(13,3),RATE(13) /285,190,120,3.13/
2202: C WRITE(*,1)((X(I,J),J=1,K),RATE(I),I=1,N)
2203: C 1 FORMAT(4F8.2)
2204: DO J=1,M
2205: IF (DABS(A(J)) .GT. 5.D00) THEN
2206: CALL RANDOM(RAND)
2207: A(J)=(RAND-0.5D00)*10.D00
2208: ENDDIF
2209: ENDDO
2210: F=0.D00
2211: DO I=1,N

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2212:      D=1.D00
2213:      DO J=1,K
2214:          D=D+A(J+1)*X(I,J)
2215:      ENDDO
2216:      FX=(A(1)*X(I,2)-X(I,3)/A(M))/D
2217: C      FX=(A(1)*X(I,2)-X(I,3)/A(5))/(1.D00+A(2)*X(I,1)+A(3)*X(I,2)+
2218: C      A(4)*X(I,3))
2219:      F=F+(RATE(I)-FX)**2
2220:      ENDDO
2221:      RETURN
2222:      END
2223: C      -----
2224:      SUBROUTINE GIUNTA(M,X,F)
2225:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2226:      DIMENSION X(*)
2227: C      GIUNTA FUNCTION
2228: C      X(I) = -1 TO 1; M=2
2229:      DO I=1,M
2230:          IF (DABS(X(I)).GT.1.D00) THEN
2231:              CALL RANDOM(RAND)
2232:              X(I)=(RAND-0.5D00)*2.D00
2233:          ENDIF
2234:      ENDDO
2235:      C=16.D00/15.D00
2236:      F=DSIN(C*X(1)-1.D0)+DSIN(C*X(1)-1.D0)**2+DSIN(4*(C*X(1)-1.D0))/50+
2237: &DSIN(C*X(2)-1.D0)+DSIN(C*X(2)-1.D0)**2+DSIN(4*(C*X(2)-1.D0))/50+.6
2238:      RETURN
2239:      END
2240: C      -----
2241:      SUBROUTINE EGGHOLD(M,X,F)
2242: C      EGG HOLDER FUNCTION
2243:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2244:      DIMENSION X(*)
2245:      DO I=1,M
2246:          IF (DABS(X(I)).GT.512.D00) THEN
2247:              CALL RANDOM(RAND)
2248:              X(I)=(RAND-0.5D00)*1024.D00
2249:          ENDIF
2250:      ENDDO
2251:      F=0.D00
2252:      DO I=1,M-1
2253:          F1=-(X(I+1)+47.D00)
2254:          F2=DSIN( DSQRT( DABS( X(I+1)+X(I)/2+47.D00 ) ) )
2255:          F3=DSIN( DSQRT( DABS( X(I)-(X(I+1)+47.D00) ) ) )
2256:          F4=-X(I)
2257:          F=F+ F1*F2+F3*F4
2258:      ENDDO
2259:      RETURN
2260:      END
2261: C      -----
2262:      SUBROUTINE TRID(M,X,F)
2263: C      TRID FUNCTION
2264:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2265:      DIMENSION X(*)
2266:      F1=0.D00
2267:      F2=0.D00
2268:      DO I=1, M
2269:          F1=F1+(X(I)-1.D00)**2
2270:      ENDDO
2271:      DO I=2, M
2272:          F2=F2+X(I)*X(I-1)
2273:      ENDDO
2274:      F=F1-F2
2275:      RETURN
2276:      END
2277: C      -----
2278:      SUBROUTINE GRIEWANK(M,X,F)

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2279:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2280:      DIMENSION X(*)
2281: C      GRIEWANK FUNCTION
2282:      F1=0.D00
2283:      F2=1.0D00
2284:      DO I=1,M
2285:      F1=F1+X(I)**2
2286:      FI=DFLOAT(I)
2287:      F2=F2*DCOS(X(I)/DSQRT(FI))
2288:      ENDDO
2289:      F=F1/4000.D00-F2+1.0D00
2290:      RETURN
2291:      END
2292: C -----
2293:      SUBROUTINE WEIERSTRASS(M,X,F)
2294:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2295:      DIMENSION X(*)
2296:      PI=4*DATAN(1.D00)
2297: C      WEIERSTRASS FUNCTION -----
2298:      DATA AX,BX,KMAX/0.5D00,3.D00,20/
2299:      F1=0.D00
2300:      F2=0.D00
2301:
2302:      DO I=1,M
2303:      IF (DABS(X(I)).GT.0.5D00) THEN
2304:      CALL RANDOM(RAND)
2305:      X(I)=RAND-0.5D00
2306:      ENDIF
2307:      ENDDO
2308:
2309:      DO I=1,M
2310:      S=0.D00
2311:      DO KK=1,KMAX+1
2312:      K=KK-1
2313:      S=S+(AX**K*DCOS(2*PI*BX**K*(X(I)+0.5D00)))
2314:      ENDDO
2315:      F1=F1+S
2316:      ENDDO
2317:
2318:      DO KK=1,KMAX+1
2319:      K=KK-1
2320:      F2=F2+(AX**K*DCOS(2*PI*BX**K*0.5D00))
2321:      ENDDO
2322:      F=F1-M*F2
2323:      RETURN
2324:      END
2325: C -----
2326:      SUBROUTINE LEVY3(M,X,F)
2327:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2328:      DIMENSION X(*)
2329: C      LEVY # 3 (LEVY ET AL. 1981) -----
2330:      DO I=1,M
2331:      IF (DABS(X(I)).GT.10.D00) THEN
2332:      CALL RANDOM(RAND)
2333:      X(I)=(RAND-0.5D00)*20
2334:      ENDIF
2335:      ENDDO
2336:      F1=0.0D+00
2337:      F2=0.0D+00
2338:      DO I=1,5
2339:      F1=F1+(I*DCOS((I-1)*X(1)+I))
2340:      F2=F2+(I*DCOS((I+1)*X(2)+I))
2341:      ENDDO
2342:      F=F1*F2
2343:      RETURN
2344:      END
2345: C -----

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2346:      SUBROUTINE LEVY5(M,X,F)
2347:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2348:      DIMENSION X(*)
2349:          F1=0.0D+00
2350:          F2=0.0D+00
2351:          DO I=1,5
2352:              F1=F1+(I*DCOS((I-1)*X(1)+I))
2353:              F2=F2+(I*DCOS((I+1)*X(2)+I))
2354:          ENDDO
2355:          F3=(X(1)+1.42513D+00)**2
2356:          F4=(X(2)+0.80032D+00)**2
2357:          F=(F1*F2) + (F3+F4)
2358:          RETURN
2359:      END
2360: C -----
2361:      SUBROUTINE LEVY8(M,X,F)
2362:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2363:      DIMENSION X(*),Y(3)
2364:      PI=4*DATAN(1.D00)
2365: C LEVY # 8 FUNCTION -----
2366:          DO I=1,3
2367:              Y(I)=1.D+00+(X(I)-1.D+00)/4.D+00
2368:          ENDDO
2369:          F1=DSIN(PI*Y(1))**2
2370:          F3=(Y(3)-1.D+00)**2
2371:          F2=0.D+00
2372:          DO I=1,2
2373:              F2=F2+((Y(I)-1.D+00)**2)*(1.D+00+10.D+00*(DSIN(PI*Y(I+1))))**2)
2374:          ENDDO
2375:          F=F1+F2+F3
2376:          RETURN
2377:      END
2378: C -----
2379:      SUBROUTINE RASTRIGIN(M,X,F)
2380:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2381:      DIMENSION X(*)
2382:      PI=4*DATAN(1.D00)
2383: C RASTRIGIN'S FUNCTION
2384:      F=0.D00
2385:      DO I=1,M
2386:          F=F+ X(I)**2 -10*DCOS(2*PI*X(I)) + 10.D00
2387:      ENDDO
2388:      RETURN
2389:      END
2390: C -----
2391:      SUBROUTINE ACKLEY(M,X,F)
2392: C ACKLEY FUNCTION
2393:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2394:      DIMENSION X(*)
2395:      PI=4*DATAN(1.D00)
2396:      F=20.D00+DEXP(1.D00)
2397:      DO I=1,M
2398:          IF(X(I).LT.-15.D00 .OR. X(I).GT.30.D00) THEN
2399:              CALL RANDOM(RAND)
2400:              X(I)=(RAND-0.5D00)*90 -15.D00
2401:          ENDF
2402:      ENDDO
2403:      F1=0.D00
2404:      F2=0.D00
2405:      DO I=1,M
2406:          F1=F1+X(I)**2
2407:          F2=F2+DCOS(2*PI*X(I))
2408:      ENDDO
2409:      F1=-20*DEXP(-0.2D00*DSQRT(F1/M))
2410:      F2=-DEXP(F2/M)
2411:      F=F+F1+F2
2412:      RETURN

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2413:      END
2414: C      -----
2415:      SUBROUTINE MICHALEWICZ(M,X,F)
2416:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2417:      DIMENSION X(*)
2418: C      MICHALEWICZ FUNCTION [ 0 <= X(I) <= PI ] MP IS A PARAMETER
2419:      MP=10 ! SET IT TO THE DESIRED VALUE
2420:      PI=4*DATAN(1.D00)
2421:      DO I=1,M
2422:      IF (X(I) .LT. 0.D00 .OR. X(I) .GT. PI) THEN
2423:      CALL RANDOM(RAND)
2424:      X(I)=RAND*PI
2425:      ENDIF
2426:      ENDDO
2427:      F=0.D00
2428:      DO I=1,M
2429:      F=F-DSIN(X(I))*(DSIN(I*X(I)**2/PI))**(2*MP)
2430:      ENDDO
2431:      RETURN
2432:      END
2433: C      -----
2434:      SUBROUTINE SCHWEFEL(M,X,F)
2435: C      SCHWEFEL FUNCTION
2436:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2437:      DIMENSION X(*)
2438:      DO I=1,M
2439:      IF (DABS(X(I)) .GT. 500) THEN
2440:      CALL RANDOM(RAND)
2441:      X(I)=(RAND-0.5D00)*1000
2442:      ENDIF
2443:      ENDDO
2444:      F=0.D00
2445:      DO I=1,M
2446:      F=F+ X(I)*DSIN(DSQRT(DABS(X(I))))
2447:      ENDDO
2448:      F=418.9829D00*M - F
2449:      RETURN
2450:      END
2451: C      -----
2452:      SUBROUTINE SHUBERT(M,X,F)
2453: C      SHUBERT FUNCTION
2454:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2455:      DIMENSION X(*)
2456:      DO I=1,M
2457:      IF (DABS(X(I)) .GT. 10.D00) THEN
2458:      CALL RANDOM(RAND)
2459:      X(I)=(RAND-0.5D00)*20
2460:      ENDIF
2461:      ENDDO
2462:      F1=0.D00
2463:      F2=0.D00
2464:      DO I=1,5
2465:      F1=F1+I*DCOS((I+1.D00)*X(1)+I)
2466:      F2=F2+I*DCOS((I+1.D00)*X(2)+I)
2467:      ENDDO
2468:      F=F1*F2
2469:      RETURN
2470:      END
2471: C      -----
2472:      SUBROUTINE DIXPRICE(M,X,F)
2473: C      DIXON & PRICE FUNCTION
2474:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2475:      DIMENSION X(*)
2476:      DO I=1,M
2477:      IF (DABS(X(I)) .GT. 10.D00) THEN
2478:      CALL RANDOM(RAND)
2479:      X(I)=(RAND-0.5D00)*20

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2480:         ENDIF
2481:     ENDDO
2482:     F=0.D00
2483:     DO I=2, M
2484:     F=F + I*(2*X(I)**2-X(I-1))**2
2485:     ENDDO
2486:     F=F+(X(1)-1.D00)**2
2487:     RETURN
2488:     END
2489: C -----
2490:     SUBROUTINE SHEKEL(M,X,F)
2491: C     SHEKEL FUNCTION FOR TEST OF GLOBAL OPTIMIZATION METHODS
2492: C     MIN F (4, 4, 4, 4) = 10.02 TO 10.54 DEPENDING ON PARAMETERS
2493:     PARAMETER(NROW=10,NCOL=4, NR=9)! NR MAY BE 2 TO 10
2494:     IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2495:     DIMENSION A(NROW,NCOL),C(NROW),X(*)
2496:     DATA ((A(I,J),J=1,NCOL),I=1,NROW)/4.,4.,4.,4.,1.,1.,1.,1.,8.,8.,
2497: & 8.,8.,6.,6.,6.,6.,3.,7.,3.,7.,2.,9.,2.,9.,5.,5.,3.,3.,8.,1.,8.,
2498: & 1.,6.,2.,6.,2.,7.,3.6D00,7.,3.6D00/
2499:     DATA (C(I),I=1,NROW)/0.1D00,0.2D00,0.2D00,0.4D00,0.4D00,0.6D00,
2500: & 0.3D00,0.7D00,0.5D00,0.5D00/
2501:     F=0.D00
2502:     DO I=1,NR
2503:     S=0.D00
2504:     DO J=1,M
2505:     S=S+(X(J)-A(I,J))**2
2506:     ENDDO
2507:     F=F-1.D00/(S+C(I))
2508:     ENDDO
2509:     RETURN
2510:     END
2511: C -----
2512:     SUBROUTINE PAVIANI(M,X,F)
2513: C     PAVIANI FUNCTION : MIN F(9.3502,...,9.3502)=45.77847 APPROX
2514: C     IN THE DOMAIN 2<= X(I) <= 10 FOR I=1,2,...,10.
2515:     IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2516:     DIMENSION X(*)
2517:     DO I=1,M
2518:     IF(X(I).LE.2.D00.OR.X(I).GE.10.D00) THEN
2519:     CALL RANDOM(RAND)
2520:     X(I)=RAND*8+2.D00
2521:     ENDIF
2522:     ENDDO
2523:     F1=0.D00
2524:     F2=1.D00
2525:     DO I=1,M
2526:     F1=F1+ DLOG(X(I)-2.D00)**2+DLOG(10.D00-X(I))**2
2527:     F2=F2*X(I)
2528:     ENDDO
2529:     F=F1-F2**0.2
2530:     RETURN
2531:     END
2532: C -----
2533:     SUBROUTINE BRANIN1(M,X,F)
2534: C     BRANIN FUNCTION #1 MIN F (1, 0) = 0
2535:     IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2536:     DIMENSION X(*)
2537:     PI=4*DATAN(1.D00)
2538:     DO I=1,M
2539:     IF(DABS(X(I)).GT.10.D00) THEN
2540:     CALL RANDOM(RAND)
2541:     X(I)=(RAND-0.5D00)*20
2542:     ENDIF
2543:     ENDDO
2544:     F=(1.D00-2*X(2)+DSIN(4*PI*X(2))/2.D00-X(1))**2+(X(2)-
2545: & DSIN(2*PI*X(1))/2.D00)**2
2546:     RETURN

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2547:      END
2548: C -----
2549:      SUBROUTINE BRANIN2(M,X,F)
2550: C      BRANIN FUNCTION #2 MIN F (3.1416, 2.25)= 0.397887 APPROX
2551: C      (-3.1416, 12.250), (9.4248, 2.25) ARE OTHER SOLUTIONS
2552:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2553:      DIMENSION X(*)
2554:      PI=4*DATAN(1.D00)
2555:      IF(X(1).LT.-5.D00 .OR. X(1).GT.10.D00) THEN
2556:      CALL RANDOM(RAND)
2557:      X(1)=RAND*15-5.D00
2558:      ENDIF
2559:      IF(X(2).LT.0.D00 .OR. X(2).GT.15.D00) THEN
2560:      CALL RANDOM(RAND)
2561:      X(2)=RAND*15
2562:      ENDIF
2563:      F=(X(2)-5.D00*X(1)**2/(4*PI**2)+5*X(1)/PI-6.D00)**2 +
2564: & 10*(1.D00-1.D00/(8*PI))*DCOS(X(1))+10.D00
2565:      RETURN
2566:      END
2567: C -----
2568:      SUBROUTINE BOHACHEVSKY1(M,X,F)
2569: C      BOHACHEVSKY FUNCTION #1 : MIN F (0, 0) = 0
2570:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2571:      DIMENSION X(*)
2572:      PI=4*DATAN(1.D00)
2573:      DO I=1,M
2574:      IF(DABS(X(I)).GT.100.D00) THEN
2575:      CALL RANDOM(RAND)
2576:      X(I)=(RAND-0.5D00)*200
2577:      ENDIF
2578:      ENDDO
2579:      F=X(1)**2+2*X(2)**2-0.3D00*DCOS(3*PI*X(1))-0.4D00*DCOS(4*PI*X(2))
2580: & +0.7D00
2581:      RETURN
2582:      END
2583: C -----
2584:      SUBROUTINE BOHACHEVSKY2(M,X,F)
2585: C      BOHACHEVSKY FUNCTION #2 : MIN F (0, 0) = 0
2586:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2587:      DIMENSION X(*)
2588:      PI=4*DATAN(1.D00)
2589:      DO I=1,M
2590:      IF(DABS(X(I)).GT.100.D00) THEN
2591:      CALL RANDOM(RAND)
2592:      X(I)=(RAND-0.5D00)*200
2593:      ENDIF
2594:      ENDDO
2595:      F=X(1)**2+2*X(2)**2-0.3D00*DCOS(3*PI*X(1))*DCOS(4*PI*X(2))+0.3D00
2596:      RETURN
2597:      END
2598: C -----
2599:      SUBROUTINE BOHACHEVSKY3(M,X,F)
2600: C      BOHACHEVSKY FUNCTION #3 : MIN F (0, 0) = 0
2601:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2602:      DIMENSION X(*)
2603:      PI=4*DATAN(1.D00)
2604:      DO I=1,M
2605:      IF(DABS(X(I)).GT.100.D00) THEN
2606:      CALL RANDOM(RAND)
2607:      X(I)=(RAND-0.5D00)*200
2608:      ENDIF
2609:      ENDDO
2610:      F=X(1)**2+2*X(2)**2-0.3D00*DCOS(3*PI*X(1)+4*PI*X(2))+0.3D00
2611:      RETURN
2612:      END
2613: C -----

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2614:      SUBROUTINE EASOM(M, X, F)
2615: C      EASOM FUNCTION : 2-VARIABLES, MIN F (PI, PI) = -1.
2616:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2617:      DIMENSION X(*)
2618:      PI=4*DATAN(1.D00)
2619:      DO I=1, M
2620:      IF (DABS(X(I)) .GT. 100.D00) THEN
2621:      CALL RANDOM(RAND)
2622:      X(I)=(RAND-0.5D00)*200
2623:      ENDIF
2624:      ENDDO
2625:      F=-DCOS(X(1))*DCOS(X(2))*DEXP(-(X(1)-PI)**2 -(X(2)-PI)**2)
2626:      RETURN
2627:      END
2628: C      -----
2629:      SUBROUTINE ROSENBROCK(M, X, F)
2630: C      ROSENBROCK FUNCTION : M VARIABLE; MIN F (1, 1, ..., 1)=0
2631:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2632:      DIMENSION X(*)
2633:      DO I=1, M
2634:      IF (X(I) .LT. -5.D00 .OR. X(I) .GT. 10.D00) THEN
2635:      CALL RANDOM(RAND)
2636:      X(I)=RAND*15-5.D00
2637:      ENDIF
2638:      ENDDO
2639:      F=0.D00
2640:      DO I=1, M-1
2641:      F=F+ (100.D00*(X(I+1)-X(I)**2)**2 + (X(I)-1.D00)**2)
2642:      ENDDO
2643:      RETURN
2644:      END
2645: C      -----
2646:      SUBROUTINE CROSSLEG(M, X, F)
2647:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2648:      DIMENSION X(*)
2649: C      CROSS-LEGGED TABLE FUNCTION ; -10<= X(I) <=10; M=2
2650: C      MIN F(0, X) OR F(X, 0) = -1.
2651:      PI=4*DATAN(1.D00)
2652:      DO I=1, M
2653:      IF ( DABS(X(I)) .GT. 10.D00) THEN
2654:      CALL RANDOM(RAND)
2655:      X(I)=(RAND-0.5D00)*20
2656:      ENDIF
2657:      ENDDO
2658:      F=- (DABS(DSIN(X(1))*DSIN(X(2))*DEXP(DABS(100.D00-(DSQRT
2659:      & (X(1)**2+X(2)**2)/PI))))+1.D00)**(-.1)
2660:      RETURN
2661:      END
2662: C      -----
2663:      SUBROUTINE CROSS(M, X, F)
2664:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2665:      DIMENSION X(*)
2666: C      CROSS FUNCTION ; -10<= X(I) <=10; M=2;
2667: C      MIN F(A, B)=0 APPROX; A, B=1.3494 APPROX OF EITHER SIGN (+ OR -)
2668:      PI=4*DATAN(1.D00)
2669:      DO I=1, M
2670:      IF ( DABS(X(I)) .GT. 10.D00) THEN
2671:      CALL RANDOM(RAND)
2672:      X(I)=(RAND-0.5D00)*20
2673:      ENDIF
2674:      ENDDO
2675:      F=(DABS(DSIN(X(1))*DSIN(X(2))*DEXP(DABS(100.D00-(DSQRT
2676:      & (X(1)**2+X(2)**2)/PI))))+1.D00)**(-.1)
2677:      RETURN
2678:      END
2679: C      -----
2680:      SUBROUTINE CROSSINTRAY(M, X, F)

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2681:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2682:      DIMENSION X(*)
2683: C     CROSS IN TRAY FUNCTION ; -10<= X(I) <=10; M=2;
2684: C     MIN F(A, B)=-20626.1218 APPROX; A, B=1.3494 APPROX OF EITHER SIGN
2685:      PI=4*DATAN(1.D00)
2686:      DO I=1,M
2687:      IF ( DABS(X(I)) .GT.10.D00) THEN
2688:      CALL RANDOM(RAND)
2689:      X(I)=(RAND-0.5D00)*20
2690:      ENDIF
2691:      ENDDO
2692:      F=- (DABS(DSIN(X(1))*DSIN(X(2))*DEXP(DABS(100.D00-(DSQRT
& (X(1)**2+X(2)**2)/PI))))+1.D00)**(.1)
2694:      RETURN
2695:      END
2696: C     -----
2697:      SUBROUTINE CROWNEDCROSS(M,X,F)
2698:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2699:      DIMENSION X(*)
2700: C     CROWNED CROSS FUNCTION ; -10<= X(I) <=10; M=2; MIN F = 1
2701: C     at (0, -9.4082), (-6.2832, 0) minf =1
2702:      PI=4*DATAN(1.D00)
2703:      DO I=1,M
2704:      IF ( DABS(X(I)) .GT.10.D00) THEN
2705:      CALL RANDOM(RAND)
2706:      X(I)=(RAND-0.5D00)*20
2707:      ENDIF
2708:      ENDDO
2709:      F=(DABS(DSIN(X(1))*DSIN(X(2))*DEXP(DABS(100.D00-
& (DSQRT(X(1)**2+X(2)**2)/PI))))+1.D00)**(.1)
2711:      RETURN
2712:      END
2713: C     -----
2714:      SUBROUTINE TTHOLDER(M,X,F)
2715:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2716:      DIMENSION X(*)
2717: C     TEST-TUBE HOLDER FUNCTION ; -10<= X(I) <=10; M=2;
2718: C     MIN F([+/-]1.5706, 0) = -10.8723
2719:      PI=4*DATAN(1.D00)
2720:      DO I=1,M
2721:      IF ( DABS(X(I)) .GT.10.D00) THEN
2722:      CALL RANDOM(RAND)
2723:      X(I)=(RAND-0.5D00)*20
2724:      ENDIF
2725:      ENDDO
2726:      F=-4*DABS(DSIN(X(1))*DCOS(X(2))*DEXP(DABS(DCOS((X(1)**2+X(2)**2)/
& 200))))
2728:      RETURN
2729:      END
2730: C     -----
2731:      SUBROUTINE HOLDERTABLE(M,X,F)
2732:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2733:      DIMENSION X(*)
2734: C     HOLDER-TABLE FUNCTION ; -10<= X(I) <=10; M=2;
2735: C     MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -26.92034 APPROX
2736:      PI=4*DATAN(1.D00)
2737:      DO I=1,M
2738:      IF ( DABS(X(I)) .GT.10.D00) THEN
2739:      CALL RANDOM(RAND)
2740:      X(I)=(RAND-0.5D00)*20
2741:      ENDIF
2742:      ENDDO
2743:      F=-DABS(DCOS(X(1))*DCOS(X(2))*DEXP(DABS(1.D00-(DSQRT(X(1)**2+
& X(2)**2)/PI))))
2745:      RETURN
2746:      END
2747: C     -----

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2748:      SUBROUTINE CARROMTABLE(M,X,F)
2749:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2750:      DIMENSION X(*)
2751: C      CARROM-TABLE FUNCTION ; -10<= X(I) <=10; M=2;
2752: C      MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -24.15682 APPROX
2753:      PI=4*DATAN(1.D00)
2754:      DO I=1,M
2755:      IF( DABS(X(I)).GT.10.D00) THEN
2756:      CALL RANDOM(RAND)
2757:      X(I)=(RAND-0.5D00)*20
2758:      ENDIF
2759:      ENDDO
2760:      F=-1.D00/30*(DCOS(X(1))*DCOS(X(2))*DEXP(DABS(1.D00-
2761: & (DSQRT(X(1)**2 + X(2)**2)/PI))))**2
2762:      RETURN
2763:      END
2764: C -----
2765:      SUBROUTINE PENHOLDER(M,X,F)
2766:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2767:      DIMENSION X(*)
2768: C      PENHOLDER FUNCTION ; -11<= X(I) <=11; M=2;
2769: C      MIN F ([+/-] 9.64617, [+/-] 9.64617) APPROX = -0.963535 APPROX
2770:      PI=4*DATAN(1.D00)
2771:      DO I=1,M
2772:      IF( DABS(X(I)).GT.11.D00) THEN
2773:      CALL RANDOM(RAND)
2774:      X(I)=(RAND-0.5D00)*22
2775:      ENDIF
2776:      ENDDO
2777:      F=-DEXP(-(DABS(DCOS(X(1))*DCOS(X(2))*DEXP(DABS(1.D0-(DSQRT
2778: & (X(1)**2+X(2)**2)/PI))))**(-1)))
2779:      RETURN
2780:      END
2781: C -----
2782:      SUBROUTINE BIRD(M,X,F)
2783:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2784:      DIMENSION X(*)
2785: C      BIRD FUNCTION ; -2PI<= X(I) <=2PI; M=2;
2786: C      MIN F (4.70104, 3.15294) APPROX = -106.764537 APPROX OR
2787: C      MIN F (-1.58214, -3.13024) APPROX = -106.764537 APPROX
2788:      PI=4*DATAN(1.D00)
2789:      DO I=1,M
2790:      IF( DABS(X(I)).GT.2*PI) THEN
2791:      CALL RANDOM(RAND)
2792:      X(I)=(RAND-0.5D00)*4*PI
2793:      ENDIF
2794:      ENDDO
2795:      F=(DSIN(X(1))*DEXP((1.D00-DCOS(X(2)))**2) +
2796: & DCOS(X(2))*DEXP((1.D00-DSIN(X(1)))**2))+(X(1)-X(2))**2
2797:      RETURN
2798:      END
2799: C -----
2800:      SUBROUTINE CHICHINADZE(M,X,F)
2801:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2802:      DIMENSION X(*)
2803: C      CHICHINADZE FUNCTION : -30 <=X(I)<= 30; M=2
2804: C      MIN F (5.901329, 0.5) = -43.3158621
2805:      PI=4*DATAN(1.D00)
2806:      DO I=1,M
2807:      IF( DABS(X(I)).GT.30) THEN
2808:      CALL RANDOM(RAND)
2809:      X(I)=(RAND-0.5D00)*60
2810:      ENDIF
2811:      ENDDO
2812:      F=X(1)**2-12*X(1)+11.D00+10*DCOS(PI*X(1)/2)+8*DSIN(5*PI*X(1))-
2813: & (1.D00/DSQRT(5.D00))*DEXP(-(X(2)-0.5D00)**2/2)
2814:      RETURN

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2815:      END
2816: C -----
2817:      SUBROUTINE MCCORMICK(M,X,F)
2818:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2819:      DIMENSION X(*)
2820: C      MCCORMICK FUNCTION : -1.5<= X(1)<=4; -3<=X(2)<=4 ; M=2
2821: C      MIN F (-0.54719755, -1.54719755) = -1.913223 APPROX
2822:      IF(X(1).LT. -1.5D00 .OR. X(1) .GT. 4.D00) THEN
2823:          CALL RANDOM(RAND)
2824:          X(1)=RAND*5.5D00-1.5D00
2825:      ENDIF
2826:      IF(X(2).LT. -3.D00 .OR. X(2) .GT. 4.D00) THEN
2827:          CALL RANDOM(RAND)
2828:          X(2)=RAND*7.D00-3.D00
2829:      ENDIF
2830:      F=DSIN(X(1)+X(2))+(X(1)-X(2))**2-1.5*X(1)+2.5*X(2)+1.D00
2831:      RETURN
2832:      END
2833: C -----
2834:      SUBROUTINE FENTONEASON(M,X,F)
2835:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2836:      DIMENSION X(*)
2837: C      FENTON & EASON FUNCTION FMIN(1.74345, -2.029695) = 1.744152
2838:      DO I=1,M
2839:          IF(DABS(X(I)).GT.100.D00) THEN
2840:              CALL RANDOM(RAND)
2841:              X(I)=(RAND-0.5D00)*200
2842:          ENDIF
2843:      ENDDO
2844:      F=1.2D00+0.1*X(1)**2 + (0.1D00+0.1*X(2)**2)/X(1)**2+
2845:      & (.1*X(1)**2*X(2)**2+10.D00)/((X(1)*X(2))**4)
2846:      RETURN
2847:      END
2848: C -----
2849:      SUBROUTINE WOOD(M,X,F)
2850:      IMPLICIT DOUBLE PRECISION (A-H,O-Z)
2851:      COMMON /RNDM/IU,IV
2852:      INTEGER IU,IV
2853:      DIMENSION X(*)
2854: C      WOOD FUNCTION:FMIN(0.443546,-0.194607,1.466077,2.15115)=1.09485393
2855:      DO I=1,M
2856:          IF(DABS(X(I)).GT.5.D00) THEN
2857:              CALL RANDOM(RAND)
2858:              X(I)=(RAND-0.5D00)*10
2859:          ENDIF
2860:      ENDDO
2861:      F1=100*(X(2)+X(1)**2)**2 + (1.D0-X(1))**2 +90*(X(4)-X(3)**2)**2
2862:      F2=(1.D0-X(3))**2 +10.1*((X(2)-1.D0)**2+(X(4)-1.D0)**2)
2863:      F3=19.8*(X(2)-1.D0)*(X(4)-1.D0)
2864:      F=F1+F2+F3
2865:      RETURN
2866:      END
2867: C -----
2868:      SUBROUTINE GLANKWAHMDEE(M,X,F)
2869:      PARAMETER (N=5)
2870:      IMPLICIT DOUBLE PRECISION (A-H,O-Z)
2871:      COMMON /RNDM/IU,IV
2872:      INTEGER IU,IV
2873:      DIMENSION X(*),A(N,N), B(N)
2874: C      ----- GLANKWAHMDEE FUNCTION -----
2875: C      GLANKWAHMDEE A, LIEBMAN JS AND HOGG GL (1979) "UNCONSTRAINED
2876: C      DISCRETE NONLINEAR PROGRAMMING. ENGINEERING OPTIMIZATION 4: 95-107
2877: C      PARSOPOULOS, KE AND VRAHATIS, MN (2002) RECENT APPROACHES TO
2878: C      GLOBAL OPTIMIZATION PROBLEMS THROUGH PARTICLE SWARM OPTIMIZATION,
2879: C      NATURAL COMPUTING 1: 235-306, 2002. REPORT THE BEST OBTAINED
2880: C      FMIN (0,12,23,17,6)= -737 OR MIN F(0, 11,22,16,6)= -737
2881: C      WE GET FMIN(-.232, 11.489, 22.273, 16.540, 6.115) = -739.822991

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2882: C -----
2883: DATA ((A(I,J),J=1,N),I=1,N) /35,-20,-10,32,-10,-20, 40,-6,-31,32,
2884: & -10,-6,11,-6,-10,32,-31,-6,38,-20,-10,32,-10,-20,31/
2885: DATA (B(J),J=1,N) /-15,-27,-36,-18,-12/
2886: C -----
2887: DO I=1,M
2888: IF (DABS(X(I)).GT.100.D00) THEN
2889: CALL RANDOM(RAND)
2890: X(I)=(RAND-0.5D00)*200
2891: ENDF
2892: ENDDO
2893: F=0.D0
2894: DO J=1,M
2895: F=F+B(J)*X(J)
2896: ENDDO
2897: DO I=1,M
2898: C=0.D0
2899: DO J=1,M
2900: C=C+X(J)*A(J,I)
2901: ENDDO
2902: F=F+C*X(I)
2903: ENDDO
2904: RETURN
2905: END
2906: C -----
2907: SUBROUTINE FLETCHER(M,X,F)
2908: C FLETCHER-POWELL FUNCTION, M <= 10, ELSE IT IS VERY MUCH SLOW
2909: C SOLUTION: MIN F = 0 FOR X=(C1, C2, C3,...,CM)
2910: C PARAMETER(N=10) ! FOR DIMENSION OF DIFFERENT MATRICES AND VECTORS
2911: C IMPLICIT DOUBLE PRECISION (A-H,O-Z)
2912: C COMMON /RNDM/IU,IV
2913: C INTEGER IU,IV
2914: C DIMENSION X(*),A(N,N),B(N,N),AA(N),BB(N),AL(N),C(N),C1(N)
2915: C PI=4*DATAN(1.D00)
2916: C GENERATE A(I,J) AND B(I,J) BETWEEN (-100, 100) RANDOMLY.
2917: C C(I) = BETWEEN (-PI, PI) IS EITHER GIVEN OR RANDOMLY GENERATED.
2918: C DATA (C(I),I=1,10)/1,2,3,-3,-2,-1,0,1,2,3/ ! BETWEEN -PI AND PI
2919: C DATA (C1(I),I=1,N)/-3,-3.02,-3.01,1,1.03,1.02,1.03,-.08,.001,3/
2920: C DATA (C1(I),I=1,N)/0,0,0,0,0,0,0,0,0,0/ ! ANOTHER EXAMPLE C1 = 0
2921: C NC=0 ! DEFINE NC HERE 0 OR 1 OR 2
2922: C IF NC=0, C1 FROM DATA IS USED (THAT IS FIXED C);
2923: C IF NC=1, C IS MADE FROM C1 BY ADDING RANDOM PART - THAT IS C=C1+R
2924: C IF NC=2 THEN C IS PURELY RANDOM THAT IS C= 0 + R
2925: C IN ANY CASE C LIES BETWEEN -PI AND PI.
2926: C -----
2927: C FIND THE MAX MAGNITUDE ELEMENT IN C1 VECTOR (UPTO M ELEMENTS)
2928: C CMAX=DABS(C1(1))
2929: C DO J=2,M
2930: C IF (DABS(C1(J)).GT.CMAX) CMAX=DABS(C1(J))
2931: C ENDDO
2932: C RANGE=PI-CMAX
2933: C -----
2934: C DO J=1,M
2935: C DO I=1,M
2936: C CALL RANDOM(RAND)
2937: C A(I,J)=(RAND-0.5D00)*200.D00
2938: C CALL RANDOM(RAND)
2939: C B(I,J)=(RAND-0.5D00)*200.D00
2940: C ENDDO
2941: C IF(NC.EQ.0) AL(J)=C1(J) ! FIXED OR NON-STOCHASTIC C
2942: C IF(NC.EQ.1) THEN
2943: C CALL RANDOM(RAND)
2944: C AL(J)=C1(J)+(RAND-0.5D0)*2*RANGE ! A PART FIXED, OTHER STOCHASTIC
2945: C ENDF
2946: C IF(NC.EQ.2) THEN
2947: C CALL RANDOM(RAND)
2948: C AL(J)=(RAND-0.5D00)*2*PI ! PURELY STOCHASTIC

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2949:      ENDIF
2950:      ENDDO
2951:      DO I=1,M
2952:      AA(I)=0.D00
2953:      DO J=1,M
2954:      AA(I)=AA(I)+A(I,J)*DSIN(AL(J))+B(I,J)*DCOS(AL(J))
2955:      ENDDO
2956:      ENDDO
2957: C-----
2958:      DO I=1,M
2959:      IF(DABS(X(I)).GT.PI) THEN
2960:      CALL RANDOM(RAND)
2961:      X(I)=(RAND-0.5D00)*2*PI
2962:      ENDIF
2963:      ENDDO
2964:      DO I=1,M
2965:      BB(I)=0.D00
2966:      DO J=1,M
2967:      BB(I)=BB(I)+A(I,J)*DSIN(X(J))+B(I,J)*DCOS(X(J))
2968:      ENDDO
2969:      ENDDO
2970:      F=0.D00
2971:      DO I=1,M
2972:      F=F+(AA(I)-BB(I))**2
2973:      ENDDO
2974:      RETURN
2975:      END
2976: C-----
2977:      SUBROUTINE POWELL(M,X,F)
2978:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
2979:      DIMENSION X(*)
2980: C      POWELL FUNCTION ; -4<= X(I) <=5; M=A MULTIPLE OF 4;
2981: C      MIN F = 0.0
2982:      DO I=1,M
2983:      IF(X(I).LT.-4.D00.OR.X(I).GT.5.D00) THEN
2984:      CALL RANDOM(RAND)
2985:      X(I)=(RAND-0.5D00)*9+.5D00
2986:      ENDIF
2987:      ENDDO
2988:      M4=M/4
2989:      F=0.D00
2990:      DO I=1,M4
2991:      J=4*I
2992:      F=F+(X(J-3)+10*X(J-2))**2+5*(X(J-1)-X(J))**2+(X(J-2)-X(J-1))**4 +
2993: & 10*(X(J-3)-X(J))**4
2994:      ENDDO
2995:      RETURN
2996:      END
2997: C-----
2998:      SUBROUTINE HARTMANN(M,X,F)
2999:      PARAMETER (N=4)
3000:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3001:      DIMENSION X(*),P(N,3),A(N,3),C(N)
3002: C      HARTMANN FUNCTION
3003: C      MIN F = -3.86278 APPROX ; 0 < X < 1.
3004:      DATA ((P(I,J),J=1,3),I=1,4) /0.6890,0.1170,0.2673,0.4699,0.4387,
3005: & 0.7470,0.1091,0.8732,0.5547,0.0381,0.5743,0.8828/
3006:      DATA ((A(I,J),J=1,3),I=1,4) /3.0,10.0,30.0,0.1,10.0,35.0,3.0,
3007: & 10.0,30.0,0.1,10.0,35.0/
3008:      DATA (C(J),J=1,4) /1.0,1.2,3.0,3.2/
3009:      DO I=1,M
3010:      IF(X(I).LE.0.D00.OR.X(I).GE.1.D00) THEN
3011:      CALL RANDOM(RAND)
3012:      X(I)=RAND
3013:      ENDIF
3014:      ENDDO
3015:      F=0.D00

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3016:      DO I=1,N
3017:      S=0.D00
3018:      DO J=1,M
3019:      S=S+A(I,J)*(X(J)-P(I,J))**2
3020:      ENDDO
3021:      F=F+C(I)*DEXP(-S)
3022:      ENDDO
3023:      F=-F
3024:      RETURN
3025:      END
3026: C-----
3027:      SUBROUTINE COLVILLE(M,X,F)
3028:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3029:      DIMENSION X(*)
3030: C      COLVILLE FUNCTION ; -10<= X(I) <=10; M= 4;
3031: C      MINF(1,1,1,1)= 0.0
3032:      DO I=1,M
3033:      IF(X(I).LT.-10.D00 .OR. X(I).GT.10.D00) THEN
3034:      CALL RANDOM(RAND)
3035:      X(I)=(RAND-0.5D00)*20
3036:      ENDIF
3037:      ENDDO
3038:      F=100*(X(1)**2-X(2))**2 + (X(1)-1.D00)**2 + (X(3)-1.D00)**2+
3039: & 90*(X(3)**2-X(4))**2+10.1*((X(2)-1.D00)**2+(X(4)-1.D00)**2)+
3040: & 19.8*(X(2)-1.D00)*(X(4)-1.D00)
3041:      RETURN
3042:      END
3043: C-----
3044:      SUBROUTINE HIMMELBLAU(M,X,F)
3045:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3046:      DIMENSION X(*)
3047:      NF=0 ! SET NF = 0 MULTIPLE OPTIMA NF=1 SINGLE OPTIMUM
3048:      DO I=1,M
3049:      IF(X(I).LT.-10.D00 .OR. X(I).GT.10.D00) THEN
3050:      CALL RANDOM(RAND)
3051:      X(I)=(RAND-0.5D00)*20
3052:      ENDIF
3053:      ENDDO
3054: C      HIMMELBLAU FUNCTION. IT HAS MULTIPLE (4) GLOBAL OPTIMA : MINF=0
3055: C      (3, 2); (-2.8051, 3.1313); (3.5744, -1.8481); (-3.779, -3.283)
3056:      IF(NF.EQ.0) THEN
3057:      F=(X(1)**2+X(2)-11)**2+(X(1)+X(2)**2-7)**2
3058:      RETURN
3059:      ENDIF
3060:      IF(NF.EQ.1) THEN
3061: C      MODIFIED HIMMELBLAU FUNCTION. IT HAS ONLY ONE GLOBAL OPTIMUM
3062: C      MINF=0 AT (3,2)
3063:      F=(X(1)**2+X(2)-11)**2+(X(1)+X(2)**2-7)**2+0.1D00*((X(1)-3)**2 +
3064: 1 (X(2)-2)**2)
3065:      ENDIF
3066:      RETURN
3067:      END
3068: C-----
3069:      SUBROUTINE BEALE(M,X,F)
3070:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3071:      DIMENSION X(*)
3072:      DO I=1,M
3073:      IF(X(I).LT.-4.500 .OR. X(I).GT.4.500) THEN
3074:      CALL RANDOM(RAND)
3075:      X(I)=(RAND-0.5D00)*9
3076:      ENDIF
3077:      ENDDO
3078: C      BEALE FUNCTION ; MINF =0 AT (3, 0.5)
3079:      F1=(1.5D00-X(1)+X(1)*X(2))**2
3080:      F2=(2.25D00-X(1)+X(1)*X(2)**2)**2
3081:      F3=(2.625D00-X(1)+X(1)*X(2)**3)**2
3082:      F=F1+F2+F3

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3083:      RETURN
3084:      END
3085: C -----
3086:      SUBROUTINE BOOTH(M,X,F)
3087:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3088:      DIMENSION X(*)
3089:      DO I=1,M
3090:      IF (X(I) .LT. -10.D00 .OR. X(I) .GT. 10.D00) THEN
3091:      CALL RANDOM(RAND)
3092:      X(I) = (RAND-0.5D00) * 20
3093:      ENDIF
3094:      ENDDO
3095: C      BOOTH FUNCTION MINF (1,3) = 0
3096:      F = (X(1) + 2*X(2) - 7.0D00) ** 2 + (2*X(1) + X(2) - 5.0D00) ** 2
3097:      RETURN
3098:      END
3099: C -----
3100:      SUBROUTINE HUMP(M,X,F)
3101:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3102:      DIMENSION X(*)
3103:      DO I=1,M
3104:      IF (X(I) .LT. -5.D00 .OR. X(I) .GT. 5.D00) THEN
3105:      CALL RANDOM(RAND)
3106:      X(I) = (RAND-0.5D00) * 10
3107:      ENDIF
3108:      ENDDO
3109: C      HUMP FUNCTION MINF (0.0898, -0.7127) = -1.0316
3110:      F = 4*X(1) ** 2 - 2.1D00*X(1) ** 4 + (X(1) ** 6) / 3.D00 + X(1) * X(2) -
3111:      & 4*X(2) ** 2 + 4*X(2) ** 4
3112:      RETURN
3113:      END
3114: C -----
3115:      SUBROUTINE MATYAS(M,X,F)
3116:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3117:      DIMENSION X(*)
3118:      DO I=1,M
3119:      IF (X(I) .LT. -10.D00 .OR. X(I) .GT. 10.D00) THEN
3120:      CALL RANDOM(RAND)
3121:      X(I) = (RAND-0.5D00) * 20
3122:      ENDIF
3123:      ENDDO
3124: C      MATYAS FUNCTION MIN F (0, 0) = 0
3125:      F = 0.26D00 * (X(1) ** 2 + X(2) ** 2) - 0.48D00 * X(1) * X(2)
3126:      RETURN
3127:      END
3128: C -----
3129:      SUBROUTINE MISHRA_1(M,X,F)
3130:      IMPLICIT DOUBLE PRECISION (A-H,O-Z)
3131:      COMMON /RNDM/IU,IV
3132:      INTEGER IU,IV
3133:      DIMENSION X(*)
3134: C      MIN F (1, 1, ..., 1) = 2
3135:      DO I=1,M
3136:      IF (X(I) .LT. 0.D00 .OR. X(I) .GT. 1.D00) THEN
3137:      CALL RANDOM(RAND)
3138:      X(I) = RAND
3139:      ENDIF
3140:      ENDDO
3141:      S = 0.D00
3142:      DO I=1,M-1
3143:      S = S + X(I)
3144:      ENDDO
3145:      X(M) = (M-S)
3146:      F = (1.D00 + X(M)) ** X(M)
3147:      RETURN
3148:      END
3149: C -----

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3150:      SUBROUTINE MISHRA_2 (M, X, F)
3151:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3152:      COMMON /RNDM/IU, IV
3153:      INTEGER IU, IV
3154:      DIMENSION X (*)
3155: C      MIN F (1, 1, ..., 1) =2
3156:      DO I=1, M
3157:      IF (X(I) .LT. 0.D00 .OR. X(I) .GT. 1.D00) THEN
3158:      CALL RANDOM (RAND)
3159:      X(I)=RAND
3160:      ENDIF
3161:      ENDDO
3162:      S=0.D00
3163:      DO I=1, M-1
3164:      S=S+ (X(I)+X(I+1))/2.D00
3165:      ENDDO
3166:      X(M)=(M-S)
3167:      F=(1.D00+X(M))**X(M)
3168:      RETURN
3169:      END
3170: C      -----
3171:      SUBROUTINE ZAKHAROV (M, X, F)
3172:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3173:      COMMON /RNDM/IU, IV
3174:      INTEGER IU, IV
3175:      DIMENSION X (*)
3176: C      ZAKHAROV FUNCTION MIN F = (0, 0, ..., 0) =0
3177:      DO I=1, M
3178:      IF (X(I) .LT. -5.D00 .OR. X(I) .GT. 10.D00) THEN
3179:      CALL RANDOM (RAND)
3180:      X(I)=(RAND-.5D0)*15 + 2.5D0
3181:      ENDIF
3182:      ENDDO
3183:      F1=0.D00
3184:      F2=0.D00
3185:      DO I=1, M
3186:      F1=F1+ X(I)**2
3187:      F2=F2 + I*X(I)/2.D00
3188:      ENDDO
3189:      F=F1+F2**2+F2**4
3190:      RETURN
3191:      END
3192: C      -----
3193:      SUBROUTINE MULTIMOD (M, X, F)
3194:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3195:      COMMON /RNDM/IU, IV
3196:      INTEGER IU, IV
3197:      DIMENSION X (*)
3198: C      MULTIMODAL FUNCTION MIN F = (0, 0) = -1 : M=2
3199:      DO I=1, M
3200:      IF (X(I) .LT. -10.D00 .OR. X(I) .GT. 10.D00) THEN
3201:      CALL RANDOM (RAND)
3202:      X(I)=(RAND-.5D0)*20
3203:      ENDIF
3204:      ENDDO
3205: C      A TYPICAL MULTIMODAL FUNCTION
3206:      F=-DCOS (X(1)) *DCOS (X(2)) *DEXP (- (X(1)**2 + X(2)**2)**2/4.D00)
3207:      RETURN
3208:      END
3209: C      -----
3210:      SUBROUTINE NONLIN (M, X, F)
3211:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3212:      COMMON /RNDM/IU, IV
3213:      INTEGER IU, IV
3214:      DIMENSION X (*)
3215: C      NONLINEAR MULTIMODAL FUNCTION MIN F = 0
3216:      DO I=1, M

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3217:      IF (X(I) .LT. -10.D00 .OR. X(I) .GT. 10.D00) THEN
3218:      CALL RANDOM(RAND)
3219:      X(I) = (RAND - .5D0) * 20
3220:      ENDF
3221:      ENDDO
3222:      F = 0.D0
3223:      DO I = 2, M
3224:      F = F + DCOS(DABS(X(I) - X(I-1)) / DABS(X(I-1) + X(I)))
3225:      ENDDO
3226:      F = F + (M - 1.D00)
3227: C      IF 0.001*X(I) IS ADDED TO F, IT BECOMES UNIMODAL
3228: C      F = F + 0.001*X(I)
3229:      RETURN
3230:      END
3231: C -----
3232:      SUBROUTINE QUADRATIC(M, X, F)
3233:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3234:      COMMON /RNDM/IU, IV
3235:      INTEGER IU, IV
3236:      DIMENSION X(*)
3237: C      QUADRATIC FUNCTION MINF (0.19388, 0.48513) = -3873.7243 (M=2)
3238:      DO I = 1, M
3239:      IF (X(I) .LT. -10.D00 .OR. X(I) .GT. 10.D00) THEN
3240:      CALL RANDOM(RAND)
3241:      X(I) = (RAND - .5D0) * 200
3242:      ENDF
3243:      ENDDO
3244:      F = -3803.84 - 138.08*X(1) - 232.92*X(2) + 128.08*X(1)**2 + 203.64*X(2)**2 +
3245:      & 182.25*X(1)*X(2)
3246:      RETURN
3247:      END
3248: C -----
3249:      SUBROUTINE TRIGON(M, X, F)
3250:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3251:      COMMON /RNDM/IU, IV
3252:      INTEGER IU, IV
3253:      DIMENSION X(*)
3254: C      TRIGON FUNCTION F MIN (0, 0, 0, ..., 0) OR (PI, 0, 0, ..., 0) = 0
3255:      PI = 4 * DATAN(1.D00)
3256:      DO I = 1, M
3257:      IF (X(I) .LT. 0.D00 .OR. X(I) .GT. PI) THEN
3258:      CALL RANDOM(RAND)
3259:      X(I) = RAND * PI
3260:      ENDF
3261:      ENDDO
3262:      F = 0.D00
3263:      DO I = 2, M
3264:      F = F + (DCOS(I + 0.D00) * DSIN(X(I) - X(I-1)))**2 +
3265:      & (I - 1.D00) * (1.D0 - DCOS(X(I)))**2
3266:      ENDDO
3267:      RETURN
3268:      END
3269: C -----
3270: C -----
3271:      SUBROUTINE COMPOUND(M, X, F)
3272:      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3273:      COMMON /RNDM/IU, IV
3274:      INTEGER IU, IV
3275:      DIMENSION X(*)
3276: C      COMPOUND FUNCTION
3277:      PI = 4 * DATAN(1.D00)
3278:      DO I = 1, M
3279:      IF (X(I) .LT. -10.D00 .OR. X(I) .GT. 10.D00) THEN
3280:      CALL RANDOM(RAND)
3281:      X(I) = (RAND - .5D0) * 20
3282:      ENDF
3283:      ENDDO

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3284:      F1=DSIN(( DCOS(X(1))+DCOS(X(2)) )**2)**2
3285:      F2=DCOS(( DSIN(X(1))+DSIN(X(2)) )**2)**2
3286:      F3=DABS(DCOS(DSQRT(DABS(X(3)**2+X(4)))))**0.5 +0.01*X(3)+.01*X(4)
3287:      F=DEXP(DSIN(DCOS(F1+F3)+DCOS(F1+DCOS(F2))))
3288:      RETURN
3289:      END
-----
3290: C
3291: C      SUBROUTINE NAME(M,X,F)
3292: C      IMPLICIT DOUBLE PRECISION (A-H, O-Z)
3293: C      PI=4*DATN(1.D0) ! IF NEEDED
3294: C      DIMENSION X(*)
3295: C      **** FUNCTION ; A<= X(I) <=B; M= MA;
3296: C      MINF( , , , )= SUCH & SUCH
3297: C      DO I=1,M
3298: C      IF(X(I).LT.-10.D00 .OR. X(I).GT.10.D00) THEN
3299: C      CALL RANDOM(RAND)
3300: C      X(I)=(RAND-0.5D00)*APPROPRIATE + APPROPRATE ETC
3301: C      ENDIF
3302: C      ENDDO
3303: C      F= ETC
3304: C      RETURN
3305: C      END
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